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Association for Predictive Medicine

Real-Time Medical Digital Twins: Geometry, Simulation, and Immersive Interaction

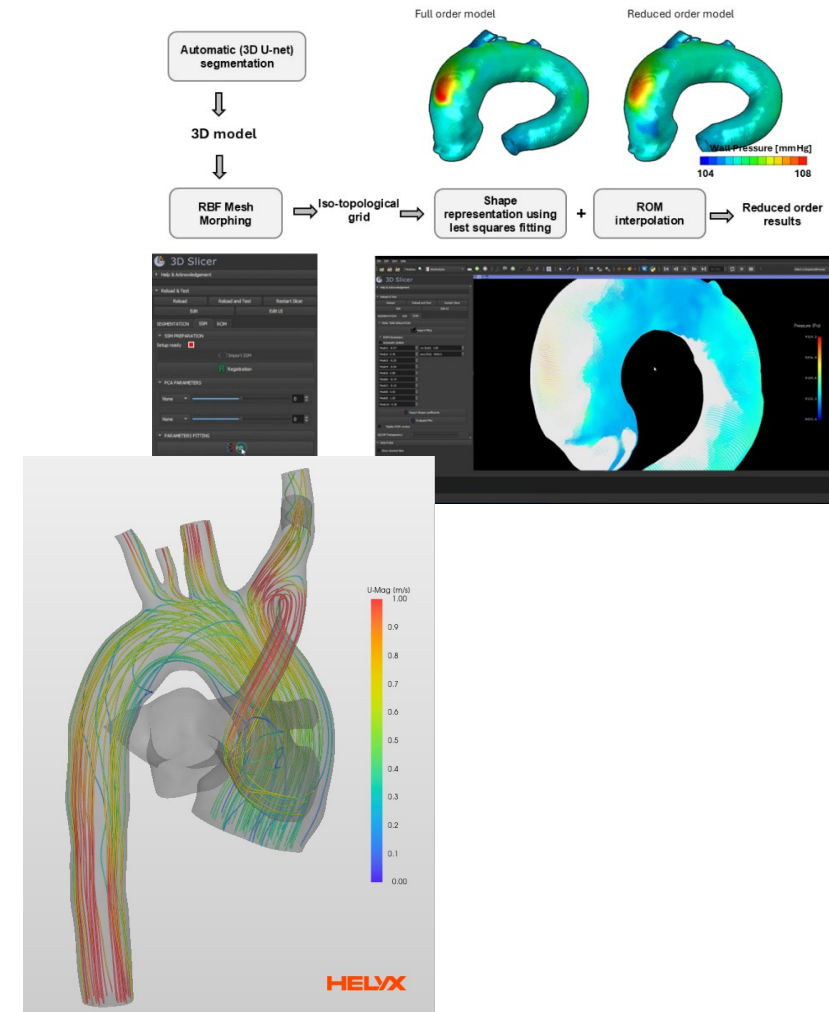
Marco Evangelos Biancolini
RBF Morph Company founder
Associate Professor





Agenda

- Digital Twins
- Radial Basis Functions
- Reduced order models
- Shape generation
- Interactive Real-Time Design Exploration
- Medical Digital Twins
 - Interactive Medical Digital Twins in 3d Slicer
 - Support to shunting procedures
- RBF Morph technologies
- Conclusions





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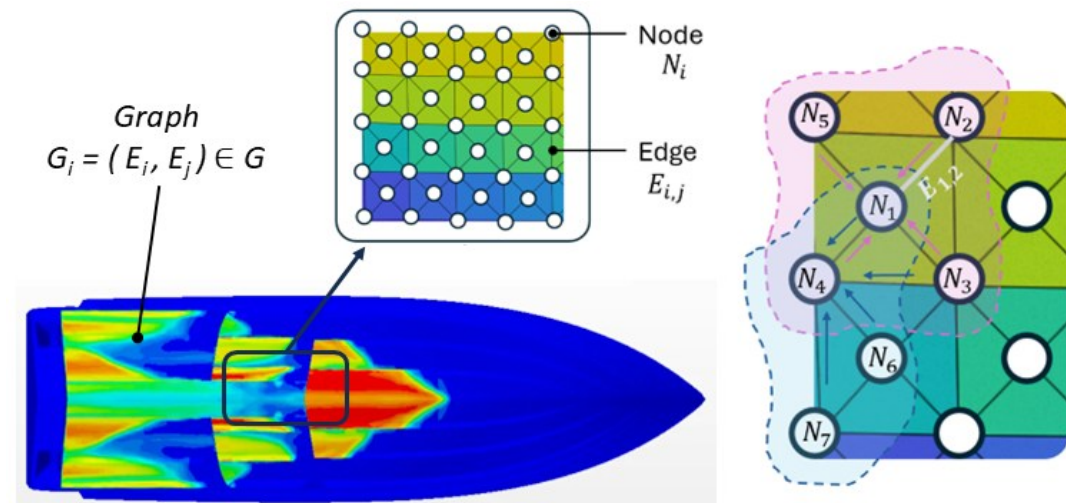
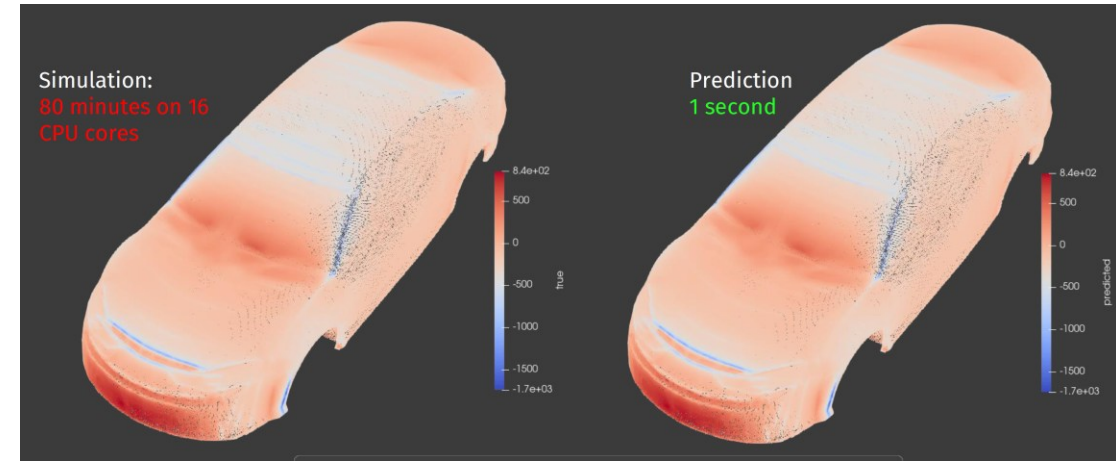
Digital Twins

Digital Engineering Applications



Digital Engineering Applications

- **Digital Twin** – digital replica of asset useful at design and operation
- CAE adoption is evolving: single verification, design variations, automated optimisation, **parametric space exploration** (snapshots)
- **Machine learning** is the reference for «AI» based approach
- High/medium fidelity simulations allow to generate the training data: **synthetic datasets**





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Radial Basis Functions

Data Science and Geometrical Intelligence



The evolution of RBF since their inception

- **Hardy** RL (1971) Multiquadric equations of topography and other irregular surfaces. *J Geophys Res* 76(8):1905–1915
- **Hardy** RL (1990) Theory and applications of the multiquadric-biharmonic method, 20 years of discovery, 1968–1988. *Comp Math Applic* 19(8/9):163–208
- **Greengard** L, Rokhlin V (1987) A fast algorithm for particle simulations. *J Comput Phys* 73:325–348
- Cipra BA (2010) The best of the 20th century: Editors name top 10 algorithms. *SIAM News Soc Ind Appl Math*. 33 (4):2. Retrieved 23 Dec
- **Powell**, M. J. (1987). Radial basis functions for multivariable interpolation: a review. *Algorithms for approximation*, 143–167.
- Powell, M. J. (1999). Recent research at Cambridge on radial basis functions. In *New Developments in Approximation Theory: 2nd International Dortmund Meeting (IDoMAT)'98, Germany, February 23–27, 1998* (pp. 215–232). Basel: Birkhäuser Basel.
- Beatson RK, Powell MJD (1993) An iterative method for thin plate spline interpolation that employs approximations to Lagrange functions. *Numerical Analysis*, Griffiths D.F & Watson G.A. (eds), London: Longmans, pp 17–39
- **Wendland** H (1995) Piecewise polynomial, positive definite and compactly supported radial basis functions of minimal degree. *Adv Comput Math* 4(1):389–396. ISSN 1019-7168
- **Babuška** I, Melenk JM (1997) The partition of unity method. *Int J Numer Meth Eng* 40(4):727–758, [https://doi.org/10.1002/\(SICI\)1097-0207\(19970228\)40:4:727::AID-NME86<3.0.CO;2-N](https://doi.org/10.1002/(SICI)1097-0207(19970228)40:4:727::AID-NME86<3.0.CO;2-N)
- Beatson RK, Greengard L (1997) A short course on fast multipole methods. In: Ainsworth M, Levesley J, Light WA, Marletta M (eds) *Wavelets, multilevel methods and elliptic PDEs*, Oxford University Press, pp 1–37
- Beatson RK, Cherrie JB, Mouat CT (1999) Fast fitting of radial basis functions: methods based on preconditioned GMRES iteration, *Adv Comput Math* 11:253–270
- Carr JC, Beatson R, Cherri J, Mitchell T, Fright W, McCallum B (2001) Reconstruction and representation of 3D objects with radial basis functions. In: *Proceedings of the 28th annual conference on Computer graphics and interactive techniques*, Los Angeles, CA, p 67–76
- Wendland H (2002) Fast evaluation of radial basis functions: methods based on partition of unity. In: Chui CK, Schumaker LL, Stöckler J (eds) *Approximation theory X: wavelets, splines, and applications*, Vanderbilt University Press, Nashville, pp 473–483
- **Faul** AC, **Goodsell** G, **Powell** MJD (2005) A Krylov subspace algorithm for multiquadric interpolation in many dimensions. *IMA J Numer Anal* 25:1–24
- **Botsch** M, Kobbelt L (2005) Real-time shape editing using radial basis functions. In: Marks J, Alexa M (eds) *Computer graphics*, 24(3), Eurographics
- Beatson RK, Powell MJD, Tan AM (2007) Fast evaluation of polyharmonic splines in three dimensions. *IMA J Numer Anal* 27:427–450. <https://doi.org/10.1093/imanum/drl027>
- Tobor I, Reuter P, Schlick C (2006) Reconstructing multi-scale variational partition of unity implicit surfaces with attributes. *Graph Models* 68(1):25–41.
- **Jakobsson** S, Amoignon O (2007) Mesh deformation using radial basis functions for gradient based aerodynamic shape optimization. *Comput Fluids* 36(6):1119–1136.
- **de Boer** A, Van der Schoot MS, Bijl H (2007) Mesh deformation based on radial basis function interpolation. *Comput Struct* 85(11–14):784–795.
- Rendall TCS, Allen CB (2009) Efficient mesh motion using radial basis functions with data reduction algorithms. *J Comput Phys* 228(17):6231–6249
- Yokota R, Barba LA (2011) Treecode and fast multipole method for n-body simulation with cuda. *GPU Comput Gems Emerald Ed*, p 113
- **Biancolini** ME (2012) Mesh morphing and smoothing by means of Radial Basis Functions (RBF): a practical example using Fluent and RBF morph. In: *Handbook of research on computational science and engineering: theory and practice*, pp 34.
- Sieger D, Menzel S, **Botsch** M (T2014) RBF morphing techniques for simulation-based design optimization. *Eng Comput* 30(2):161–174
- **Biancolini**, M. E. (2017). *Fast radial basis functions for engineering applications* (pp. 1–36). Cham: Springer International Publishing.

- Hardy – Multiquadric
- Greengard – Fast Multi Pole
- Powell – generalisation to $\mathbb{R}^n$
- Beatson – thin plate spline
- Wendland - compact support
- Babuška – Partition of Unity
- FGP – fast iterative MQ in $\mathbb{R}^n$
- Jakobsson, de Boer, morphing
- Botsch, interactive morphing
- Biancolini, LCM, first RBF industrial software
- Biancolini, Fast RBF Book



Radial Basis Functions (RBF) in a nutshell

source points

$$s(\mathbf{x}) = \sum_{i=1}^N \gamma_i \cdot \underbrace{\varphi(\|\mathbf{x} - \mathbf{x}_{k_i}\|)}_{\text{radial basis}} + \underbrace{h(\mathbf{x})}_{\text{polynomial}}$$

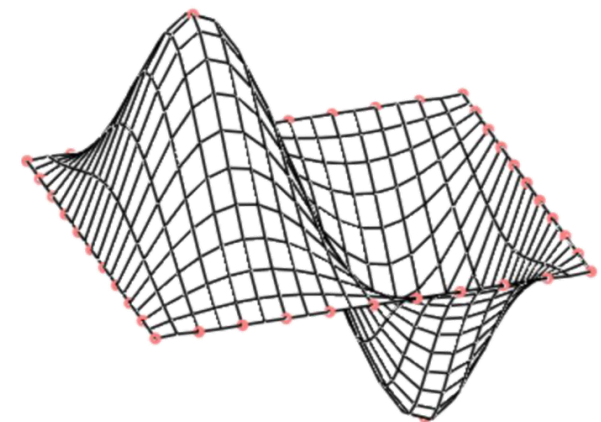
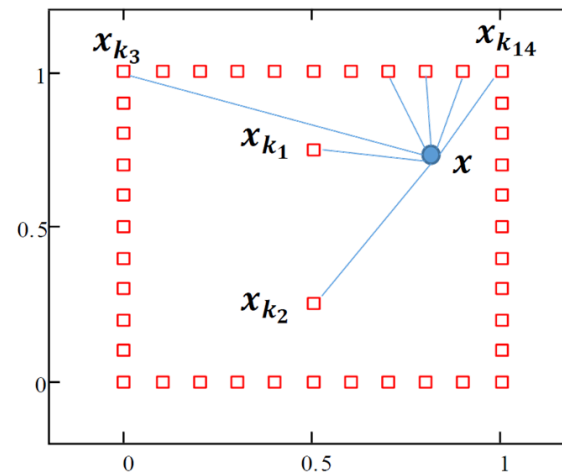
weight

e.g. $h(\mathbf{x}) = \beta_1 + \beta_2 x + \beta_3 y + \beta_4 z$

shift of the target point to the i-th data site

RBF	$\varphi(r)$
Spline type (Rn)	$r^n, n \text{ odd}$
Thin plate spline	$r^n \log(r) \text{ } n \text{ even}$
Multiquadratic (MQ)	$\sqrt{1 + r^2}$

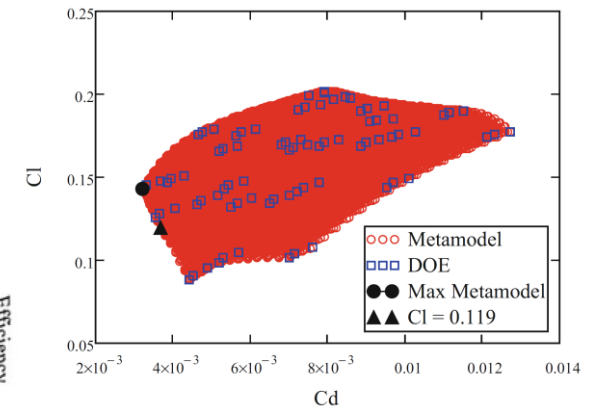
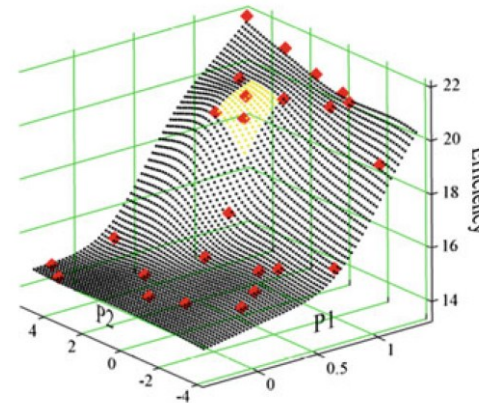
RBF are a very powerful mathematical tool able to interpolate **everywhere** in the $\mathbb{R}^n$ space a function given at scattered **source points**





Interpolators in multi-dimensional spaces

- **Data science** problems
 - **Inference** $\mathbb{R}^n \Rightarrow \mathbb{R}^m$
 - Gaussian RBF is recognized as the “RBF neural network”
 - Useful for **surrogates** in **optimization**
- 3D space manipulation (shape deformation, data mapping)
 - Field manipulation is a key enabler for **geometric intelligence**
 - RBF mapping for multi-physics interfaces and as a “morphing extender”





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Reduced order models

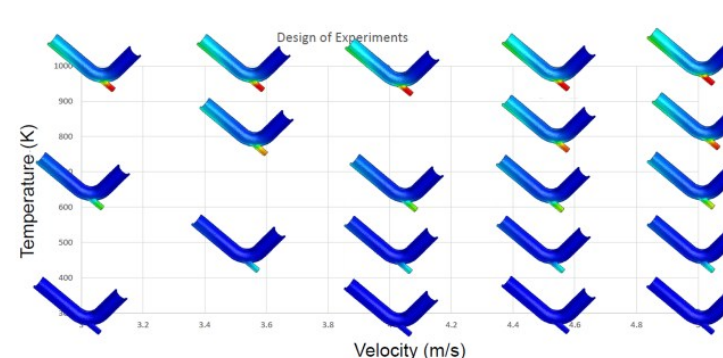
Singular Value Decomposition and Principal Orthogonal Decomposition

RBF and POD can be combined to get reduced order models (ROM)

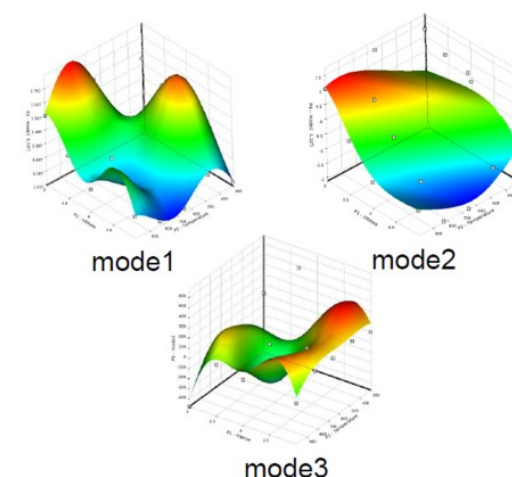


- CFD snapshot data are compressed using **Singular Value Decomposition** (SVD) and **Proper Orthogonal Decomposition** (POD).
- AI models are trained in the reduced space using **Radial Basis Functions** (RBFs).
- Full-field solutions are reconstructed via **RBF inference** and modal expansion.

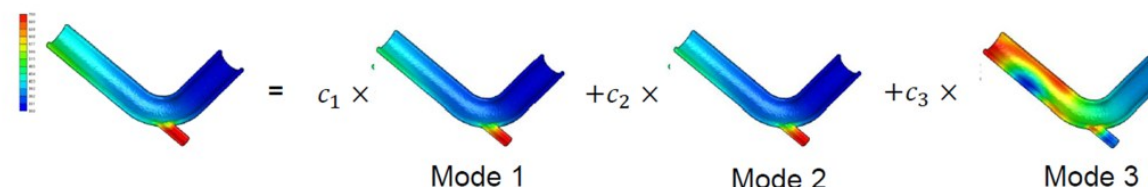
SNAPSHOTS - SVD - POD



RBF



POD + RBF = ROM





RBF and POD can be combined to get reduced order models (ROM)

- Singular Value Decomposition (Beltrami-Jordan 1873)

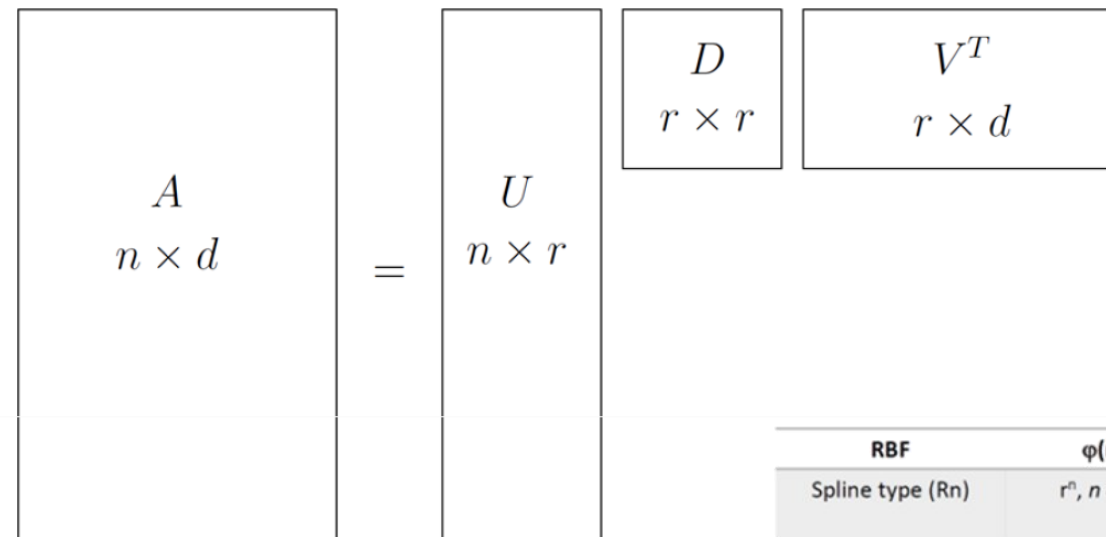
$$\mathbf{X} = \mathbf{U} \mathbf{\Sigma} \mathbf{V}^T$$

- Radial Basis Functions (Hardy 1971)

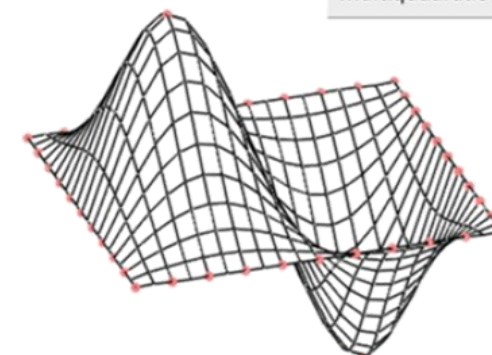
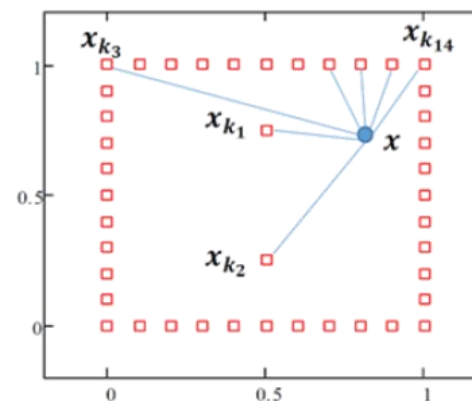
$$s(\mathbf{x}) = \sum_{i=1}^N \gamma_i \phi(\|\mathbf{x} - \mathbf{x}_i\|) + p(\mathbf{x})$$

- Reconstruction by modal expansion

$$\mathbf{A} = \sum_{i=1}^d \sigma_i \mathbf{u}_i \mathbf{v}_i^T$$



RBF	$\phi(r)$
Spline type (Rn)	$r^n, n \text{ odd}$
Thin plate spline	$r^n \log(r) \text{ } n \text{ even}$
Multiquadratic (MQ)	$\sqrt{1 + r^2}$



RBF and POD can be combined to get reduced order models (ROM)



- ROM can be originated by **geometrical and physical parameters**
 - ROM of the shape (**geometrical modes weights**) is trained vs. **input parameters**
 - ROM of the CAE solution (**CAE modes weights**) is trained vs. **input parameters**
- ROM can be originated by **multiple parameter-less snapshots** (statistical shape modeling)
 - ROM of the shape (**geometrical modes weights**) is used to train the ROM of the CAE solution (**CAE modes weights**)
 - A new shape is projected onto the ROM of the shape and the new CAE solution is inferred



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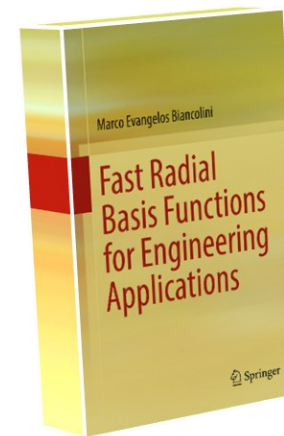
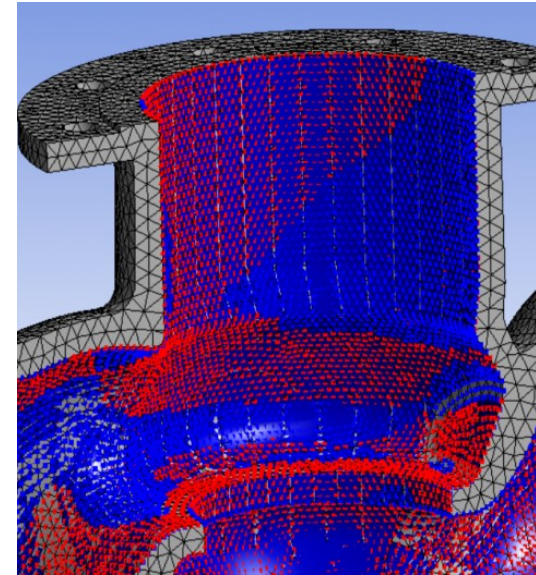
Shape generation

Parameter-based and parameter-free workflows

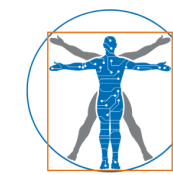


RBF Mesh Morphing

- We adopt **Radial Basis Functions** (RBF) to drive mesh morphing (smoothing) from a list of source points and their displacements
 - Surface shape changes
 - Volume mesh smoothing
- RBF are recognized to be one of the **best mathematical tool** for mesh morphing

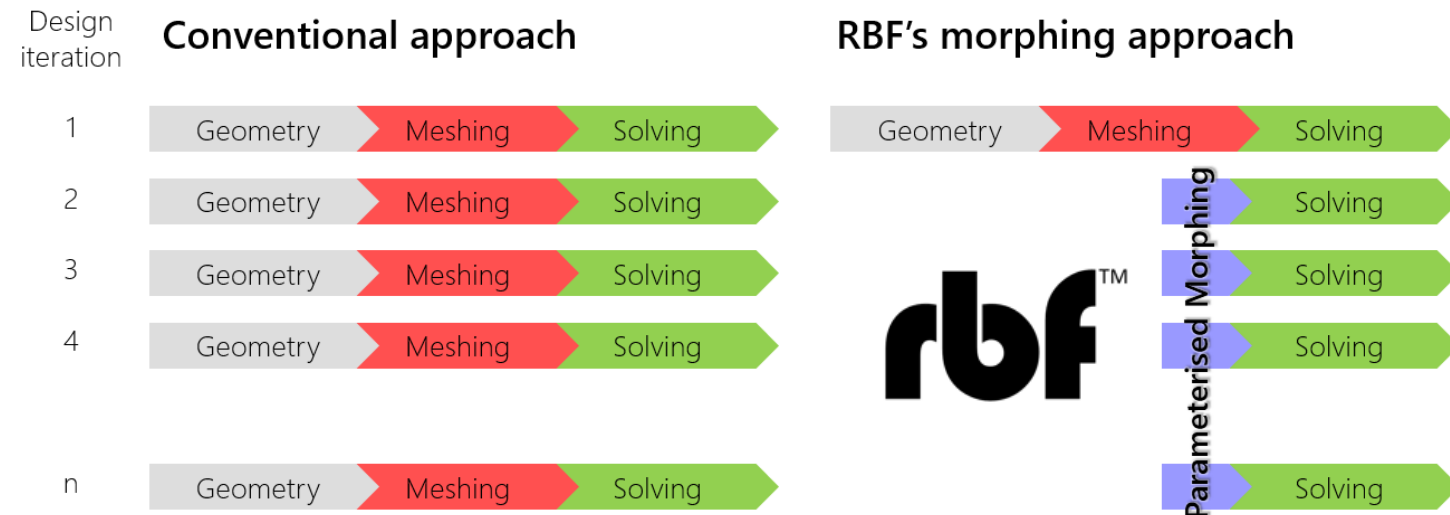


$$\begin{cases} s_x(\mathbf{x}) = \sum_{i=1}^N \gamma_i^x \varphi(\|\mathbf{x} - \mathbf{x}_{s_i}\|) \\ s_y(\mathbf{x}) = \sum_{i=1}^N \gamma_i^y \varphi(\|\mathbf{x} - \mathbf{x}_{s_i}\|) \\ s_z(\mathbf{x}) = \sum_{i=1}^N \gamma_i^z \varphi(\|\mathbf{x} - \mathbf{x}_{s_i}\|) \end{cases}$$



Automated shape generation

- Morphing is a **key enabler** for Digital Twins
- Multiple snapshots can be generated from **shape parameters**
- **Virtual shapes** can be added from SSM
- Synthetic dataset are generated with an high level of **automation**

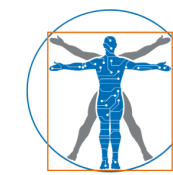




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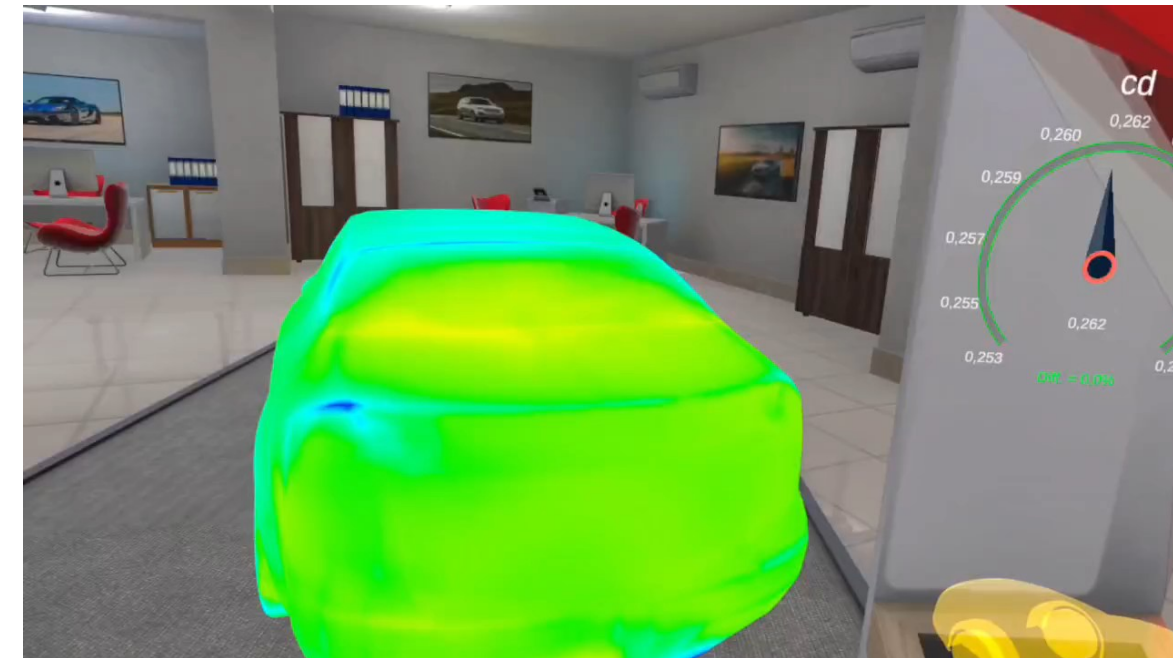
Interactive Real-Time Design Exploration

From Advanced Simulation to VR



Interactive Digital Twins?

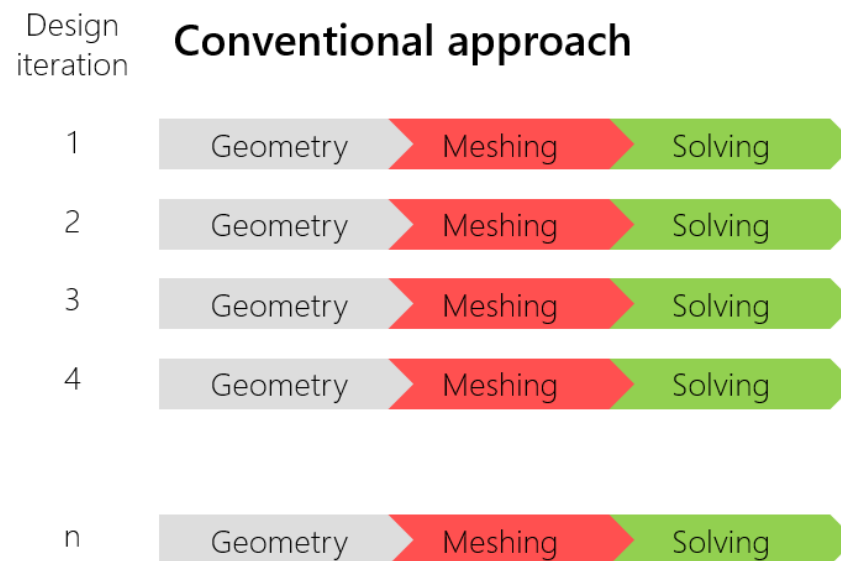
- High-fidelity simulations big data for training AI models:
 - Design stage: steer new projects more effectively
 - Operation stage: **real-time** interactions are key enablers of digital twins
- Challenges:
 - **High level of automation required**
 - **Replicable, easily deployable workflow**
- We present a comprehensive solution powered by **Unity rendering** and exported to **Meta Quest 3 AR/VR**



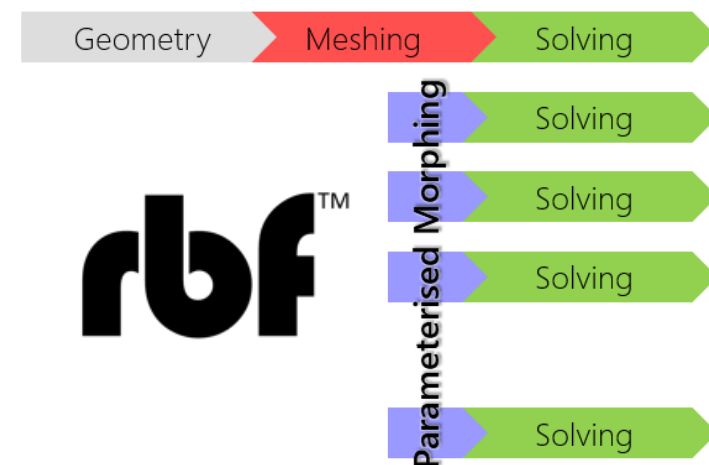


Interactive Digital Twins Challenge #1

- High level of automation to create snapshots is needed
- Geometrical parameters require mesh topology preservation
- **RBF mesh morphing** combined with **CAE solvers**



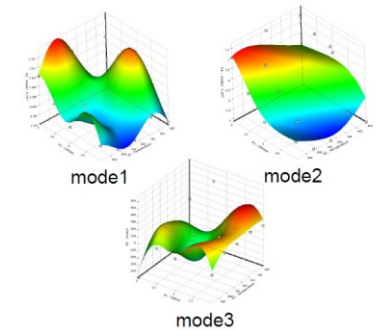
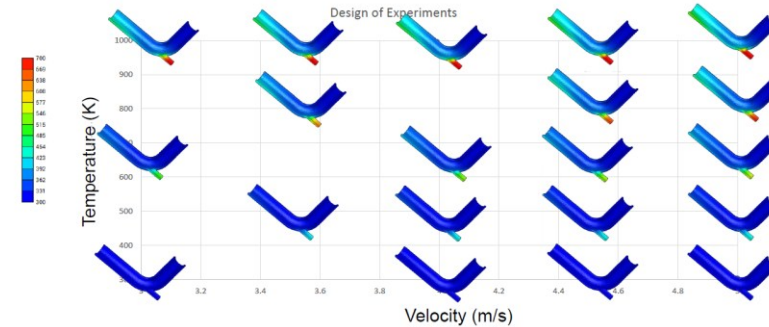
RBF's morphing approach





Interactive Digital Twins Challenge #2

- Replicable, easily deployable workflow?
- **Reduced Order Models** (ROM) are compressed (POD) ready to be inferred (GARS or RBF)
- Unity rendering
 - Meta Quest 3 AR/VR
 - Apple VisionPro?
- Portable Functional Mockup Units



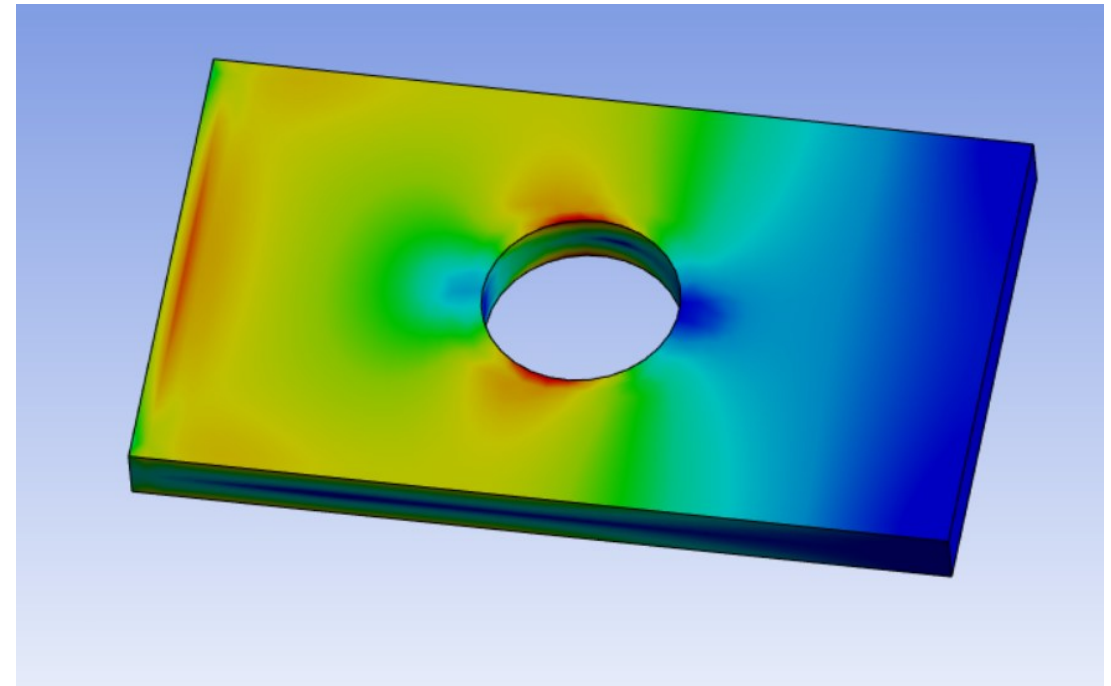
POD+GARS = ROM

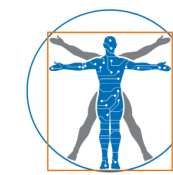
$$\text{Temperature Field} = c_1 \times \text{Mode 1} + c_2 \times \text{Mode 2} + c_3 \times \text{Mode 3}$$



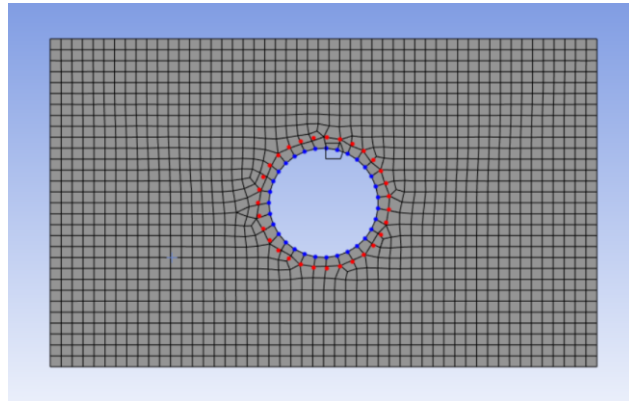
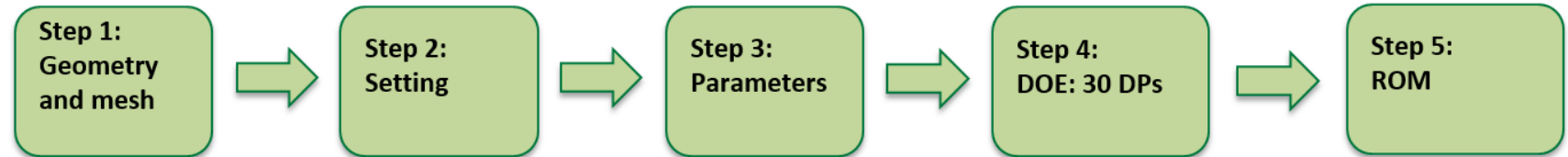
A simple FEA model – ROM – FMU

- Solid model created by CAD
- The notch effect is accurately captured by Mechanical
- RBF morphing allows to create **one geometrical parameter** to change the diameter of the hole
- The applied loads is the **physical parameter**
- Snapshots are exported and the FMU created

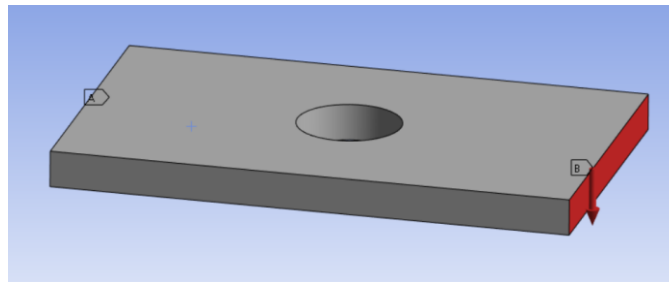




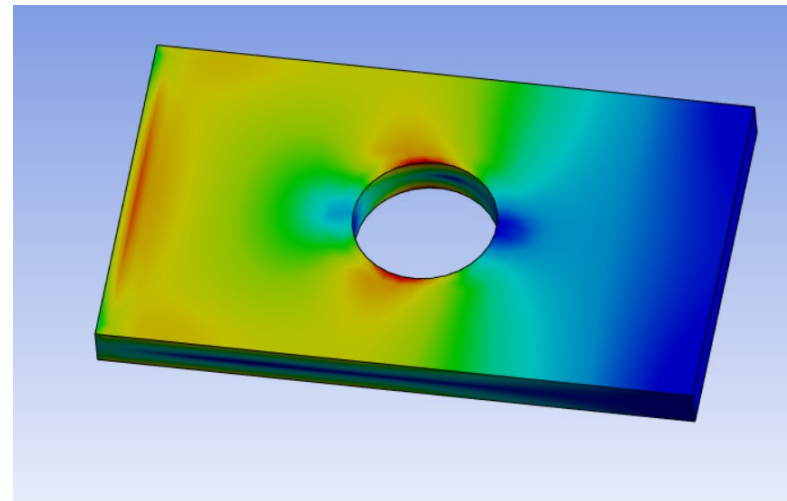
Workflow



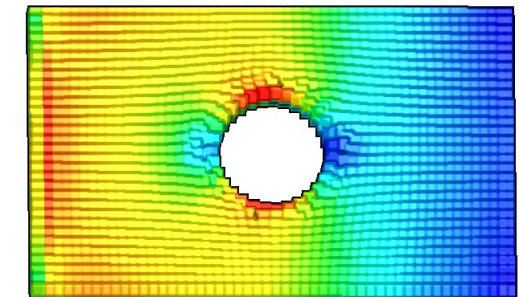
Shape parameter: radius offset



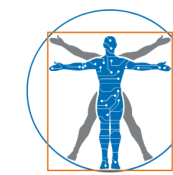
Physical parameter: Force



von Mises stresses



ROM convergence check



Twin Builder

- ROM Builder
- Input parameters are controlled by the sliders
- **Point-based** rendering

Delete

Rename

ROM Information

Name :

s

Parameters (fields) :

2 (0)

Learning Snapshots :

16

Output :

6 modes

Version :

2021R2

Export to Twin Builder

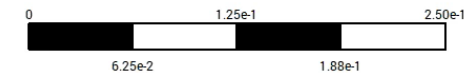
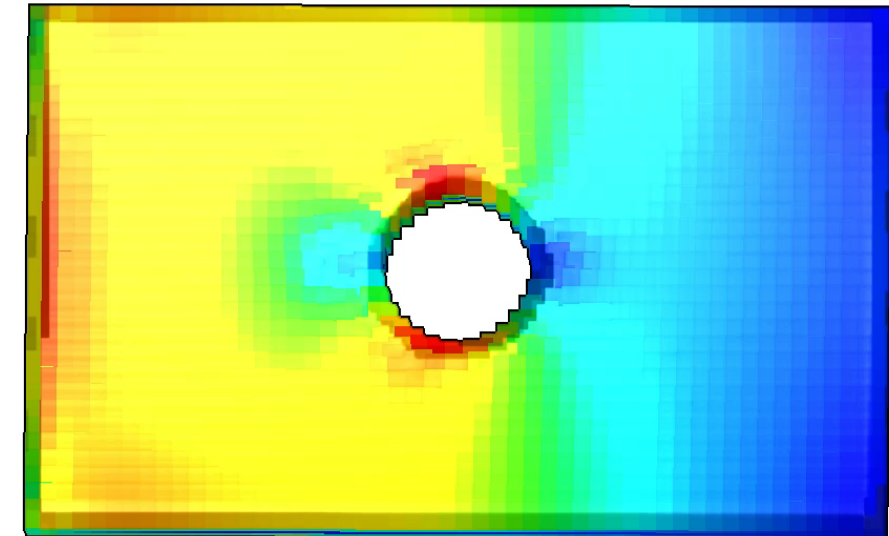
Evaluate ROM

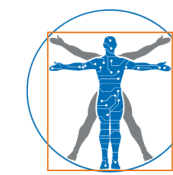
Input parameters :

Parameter	Value
offset Surface Offset	-3.11523e-03 - +
Force Y Component	-5.06608e+04 - +

Save snapshot

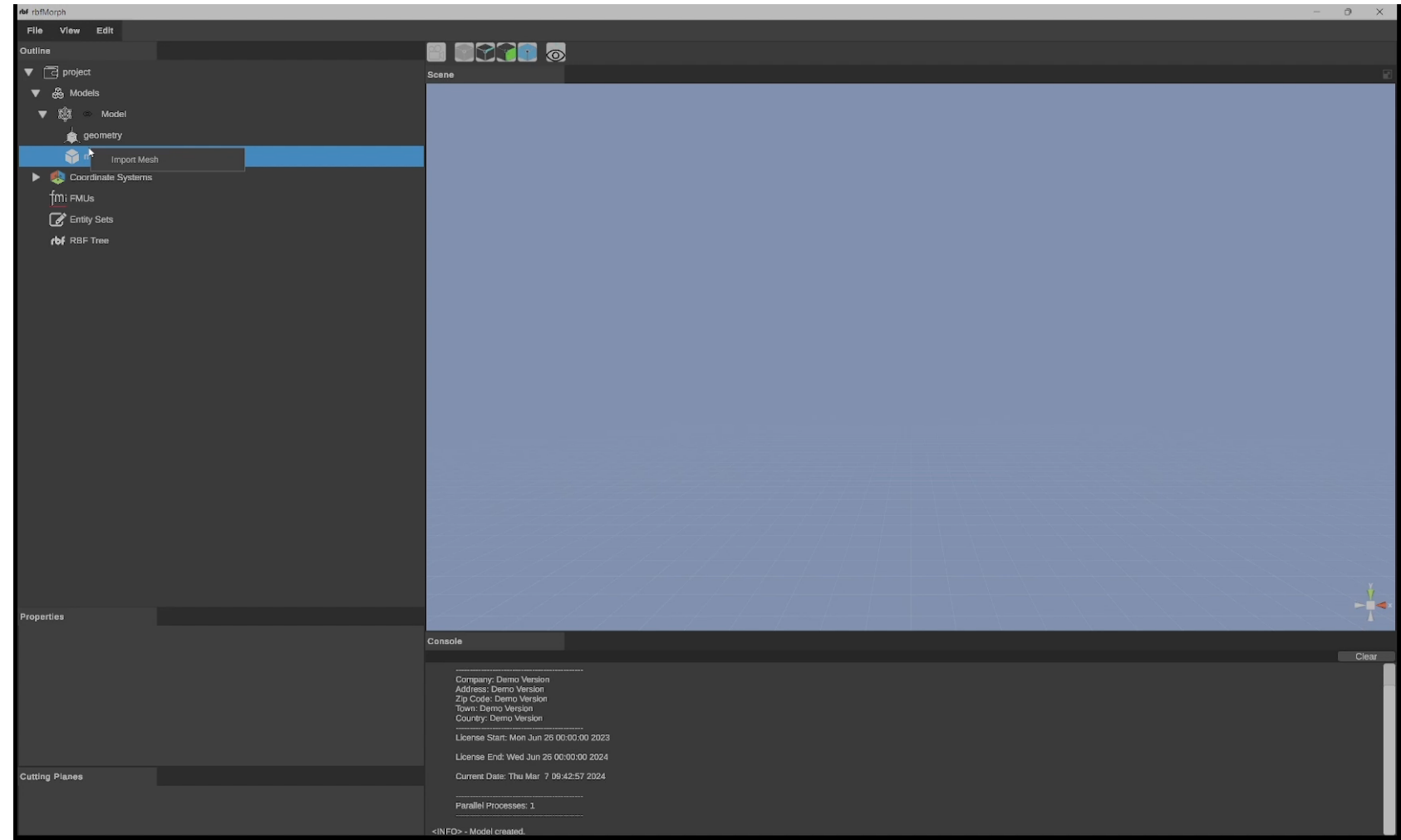
Stress (Pa)





rbfCAE Unity UI

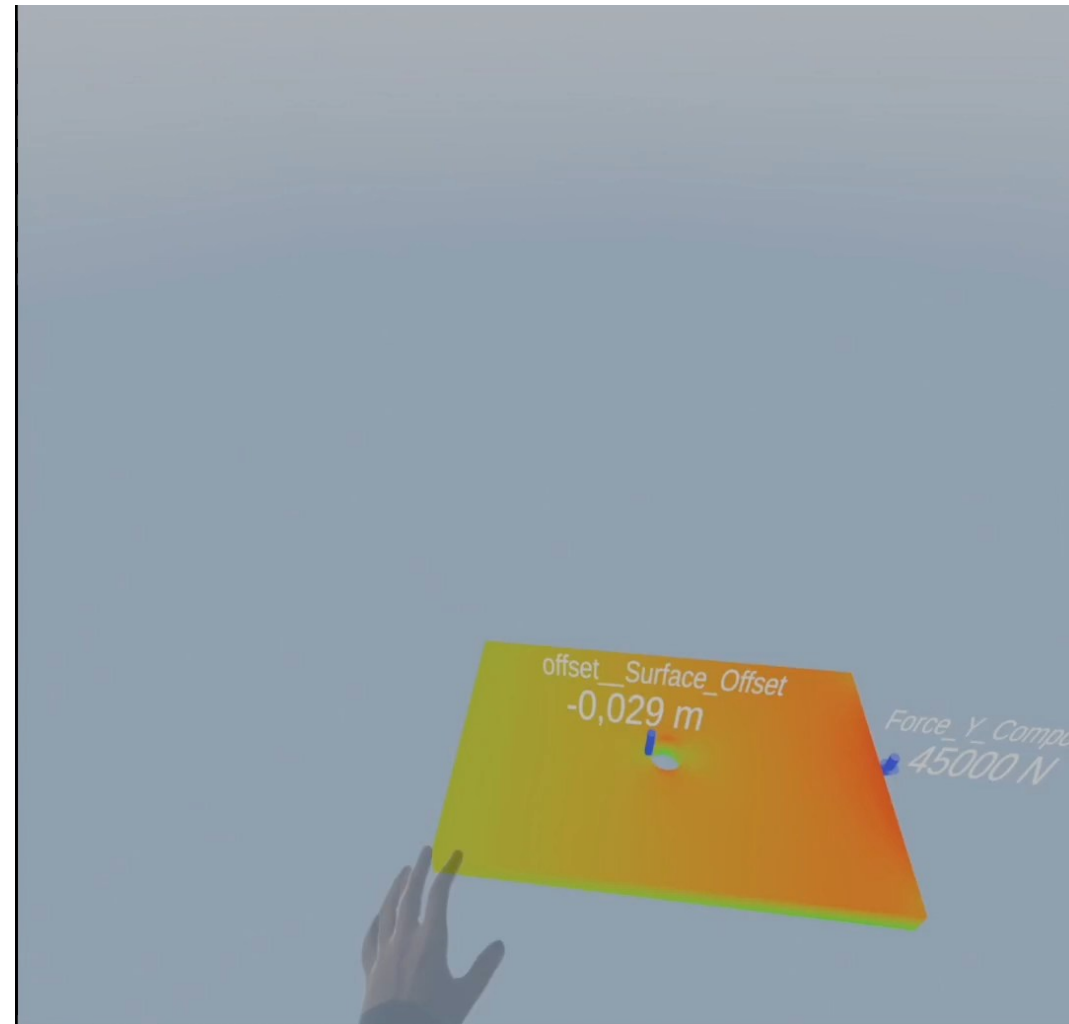
- Unity UI capable to read in **surface** and **FMU**
- Input parameters are controlled by **handles** (json descriptor)
- **Surface-based** rendering

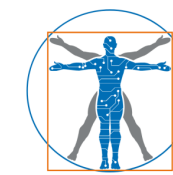




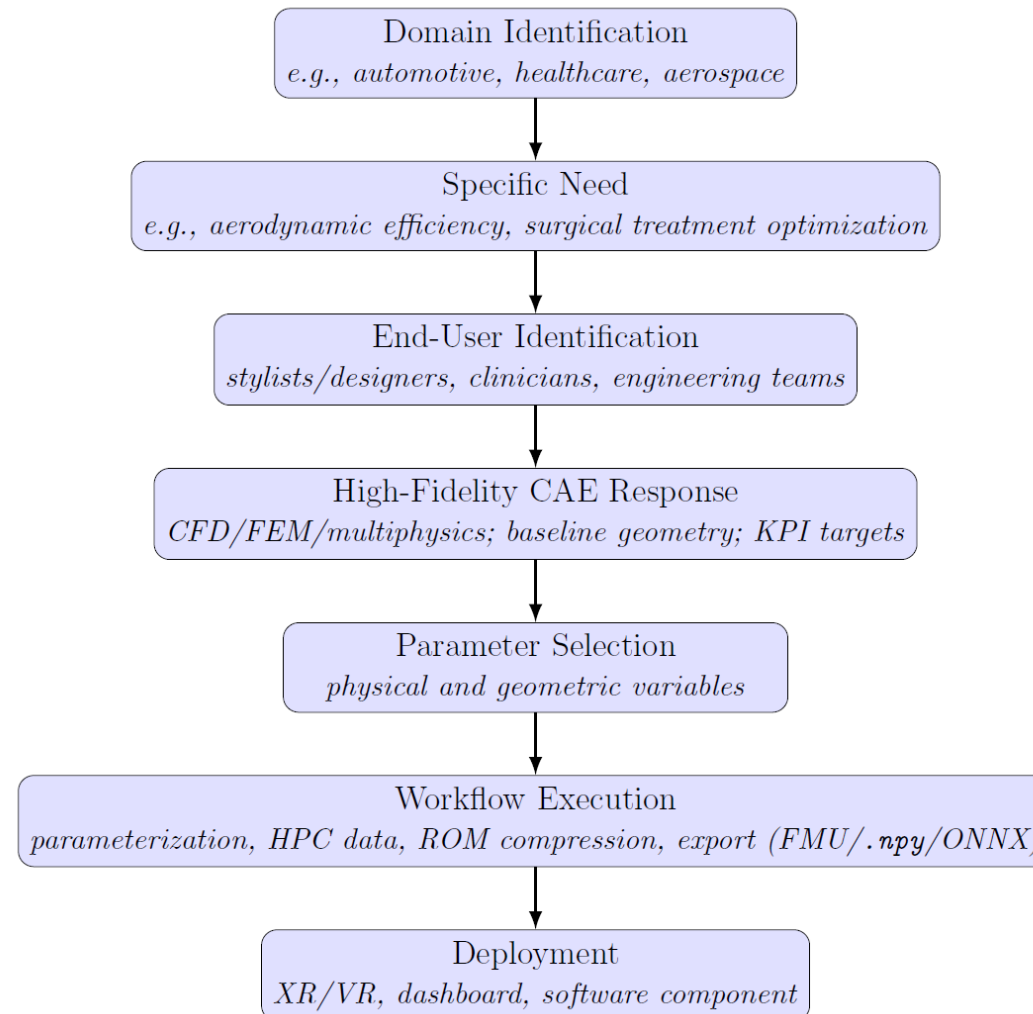
RBF Morph exported VR

- FMU are translated to ARM
- Meta Quest 3
- Input parameters are controlled by hands
- We can add an **immersive scene**
- Wireless AR/VR



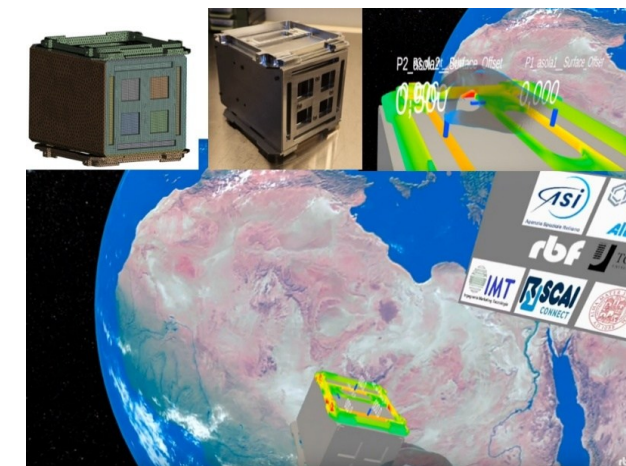
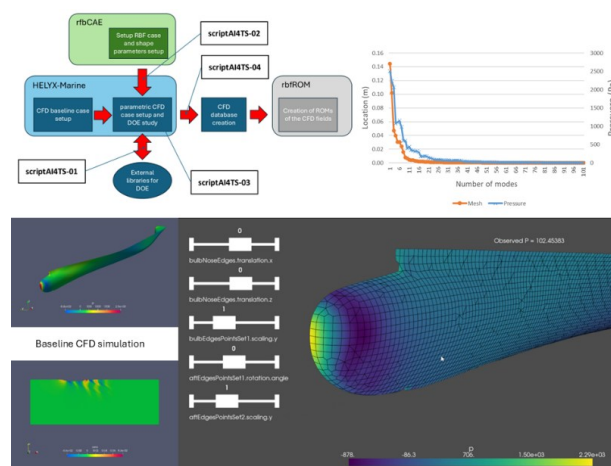
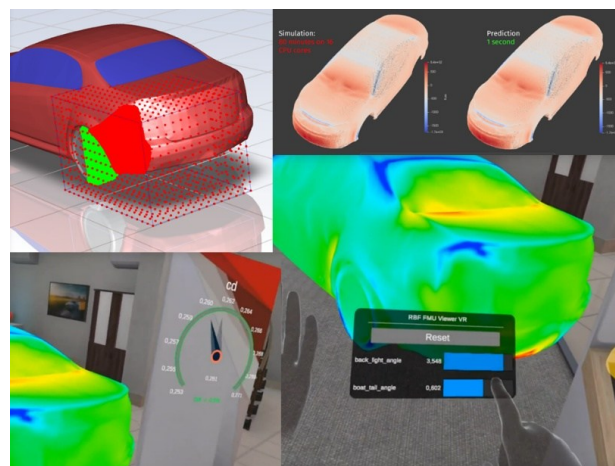
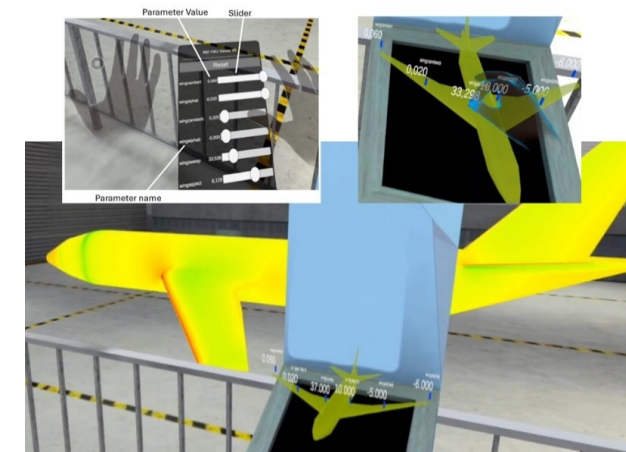
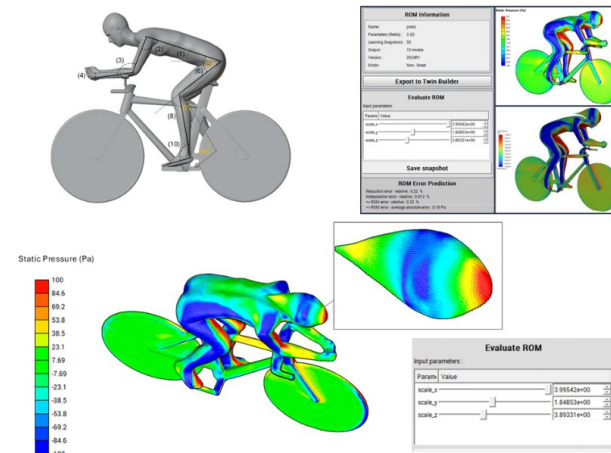
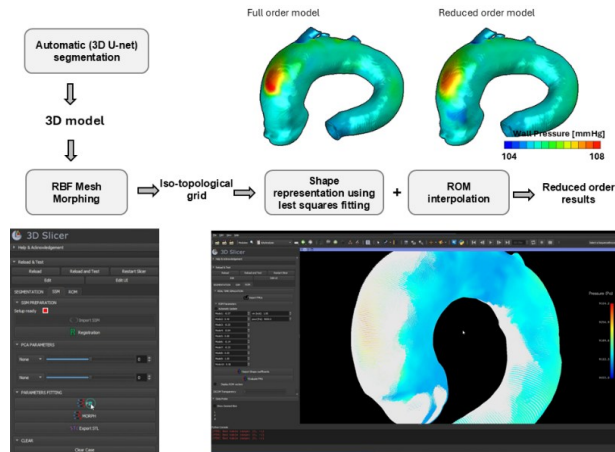


CAE agnostic approach





Interactive Real-Time Design Exploration: Applications





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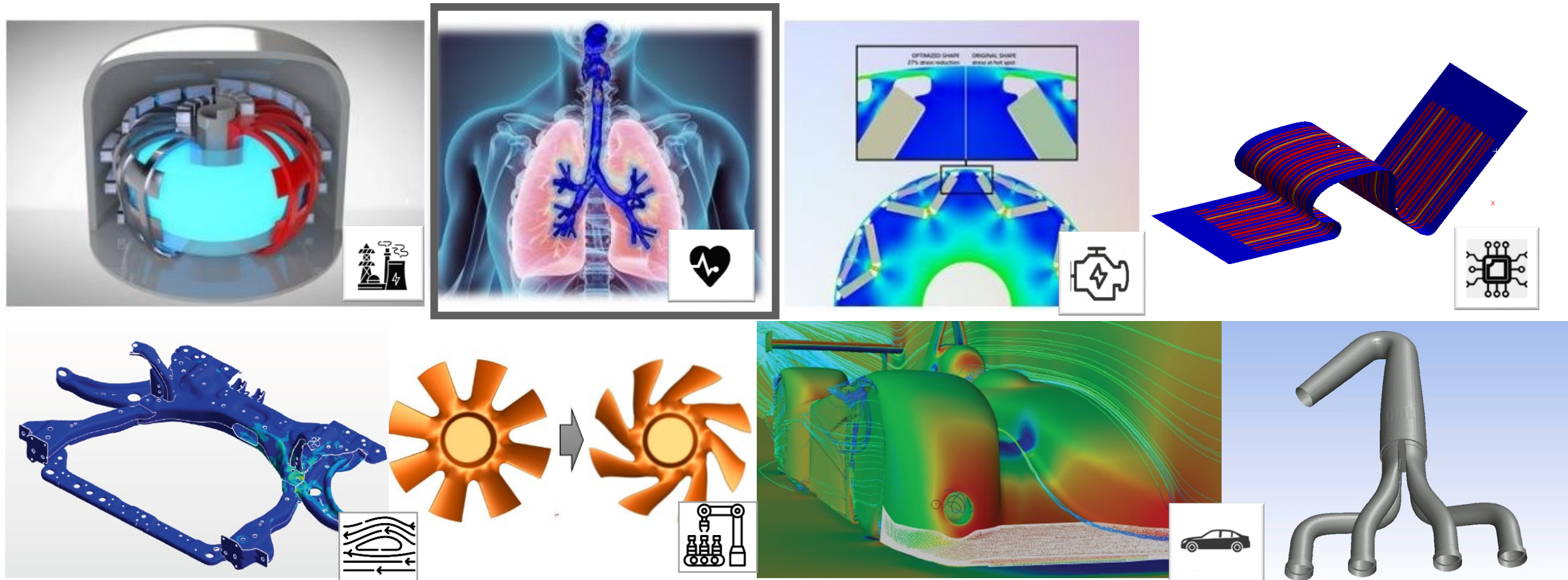
Medical Digital Twins

Research Projects and Applications

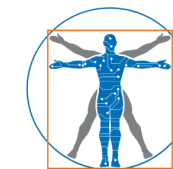
Research and Industrial sectors



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EU-funded research projects 2013-2025



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Funded by
the European Union

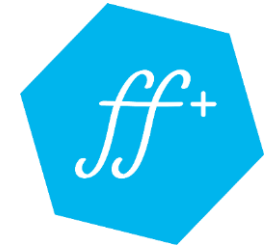


Running projects on healthcare

- Fortissimo Plus Business Experiment
PANDORA - **Pre-operative Assistant Based on Data-Driven Approaches for Vascular Grafts Surgery**
- EU-funded Cyber 4.0 competence center
SafeBot4Twin - **A Large Language Model-based Cyber-secure chatbot to control Medical Digital Twins**
- NextGenerationEU - iNEST project
ROMed2VR - **Virtual Reality Empowered by Computational Fluid Dynamics Reduced Order Models to Support Pre-Surgery Medical Planning**



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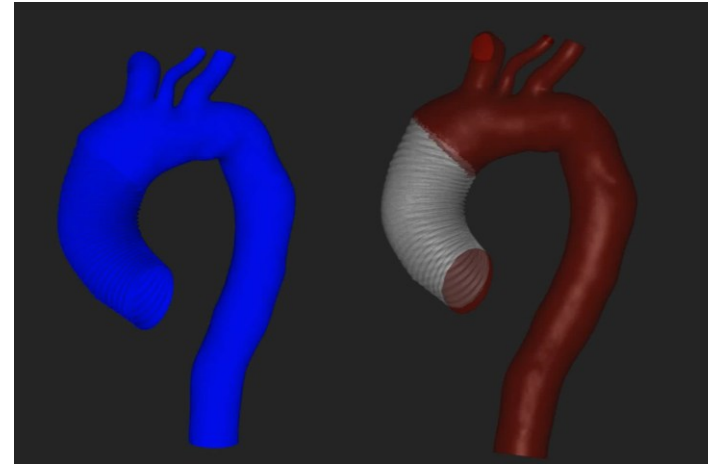
ROMed2VR

iNEST
Interconnected
Nord-Est Innovation
Ecosystem



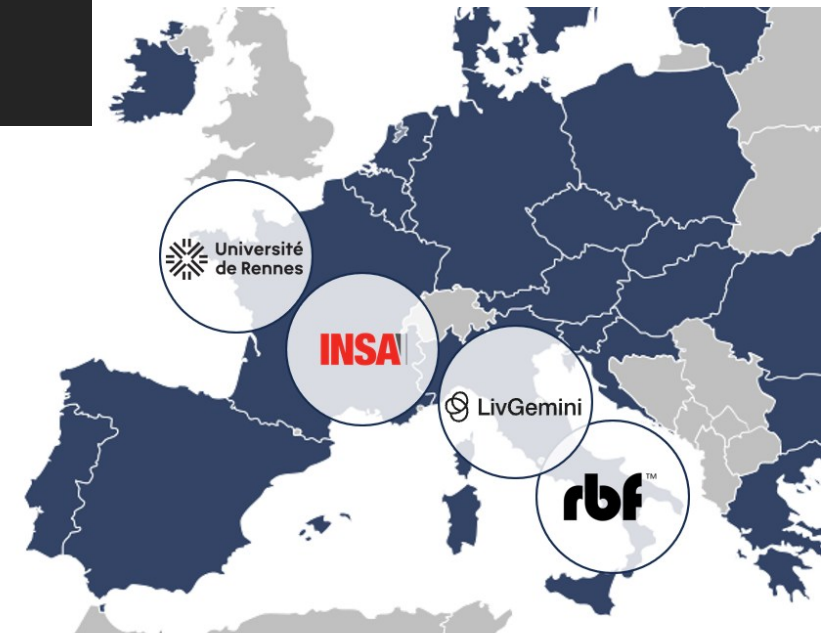


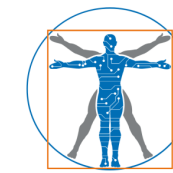
PANDORA



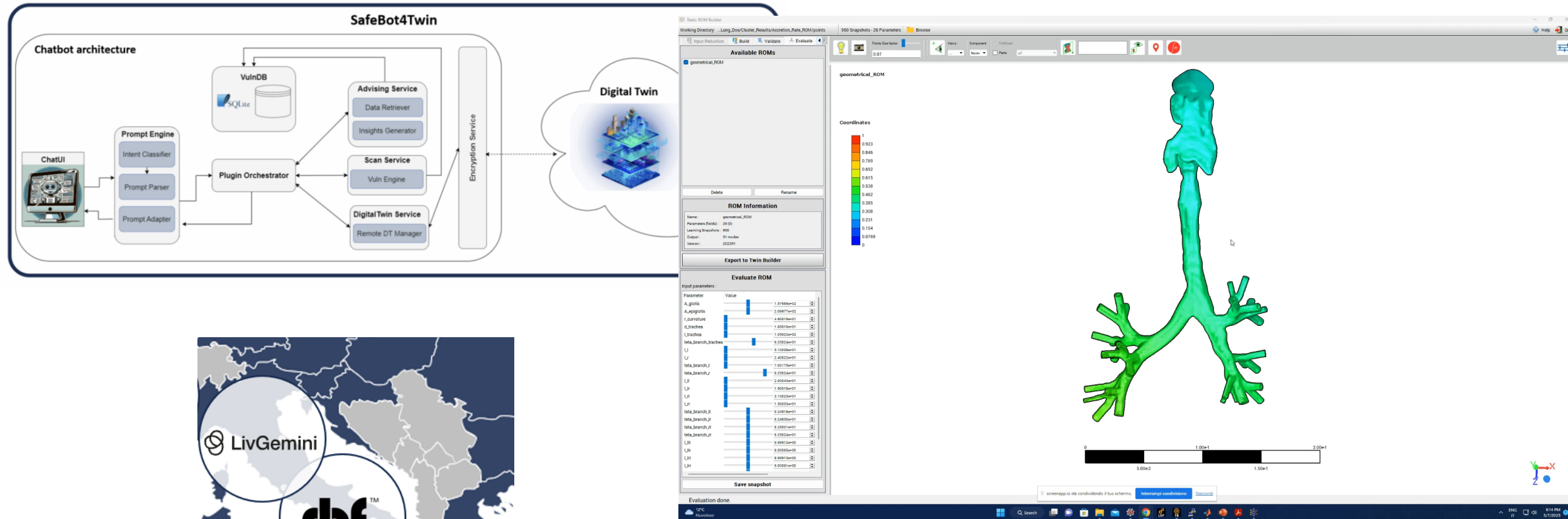
PANDORA

Pre-operative AssistaNt based on Data-driven apprOaches for vasculaR grAft surgery





SafeBot4Twin





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Association for Predictive Medicine

Interactive Medical Digital Twins in 3d Slicer

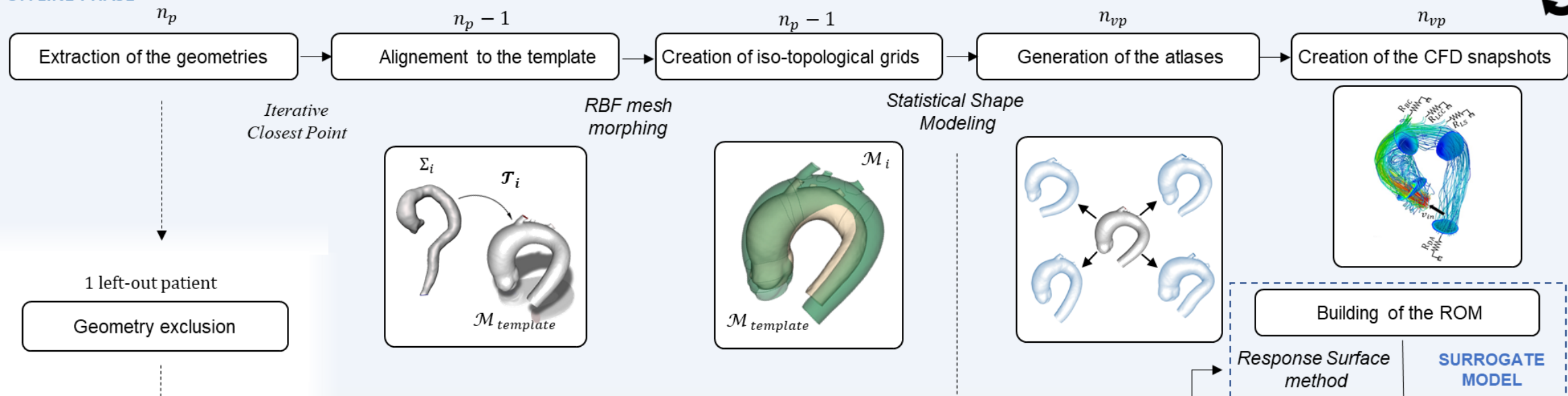
Meditate ESR02 – Leonardo Geronzi

<https://meditate-project.eu/esr-02-leonardo-geronzi/>

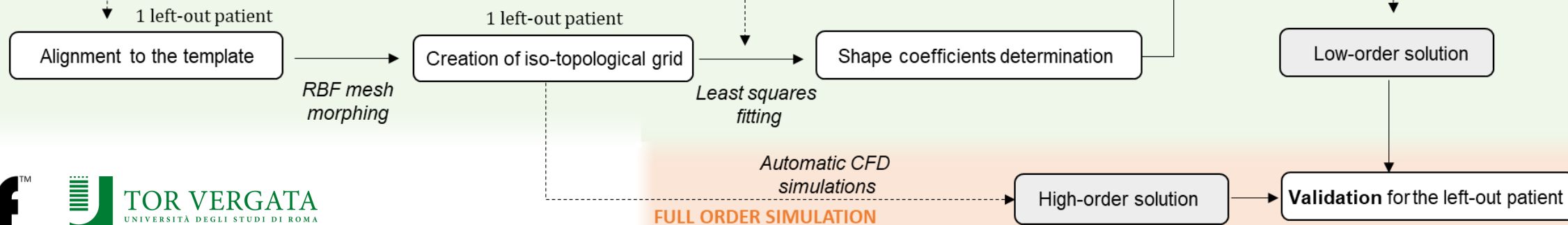


Hemodynamic prediction based on surrogate modeling

OFFLINE PHASE



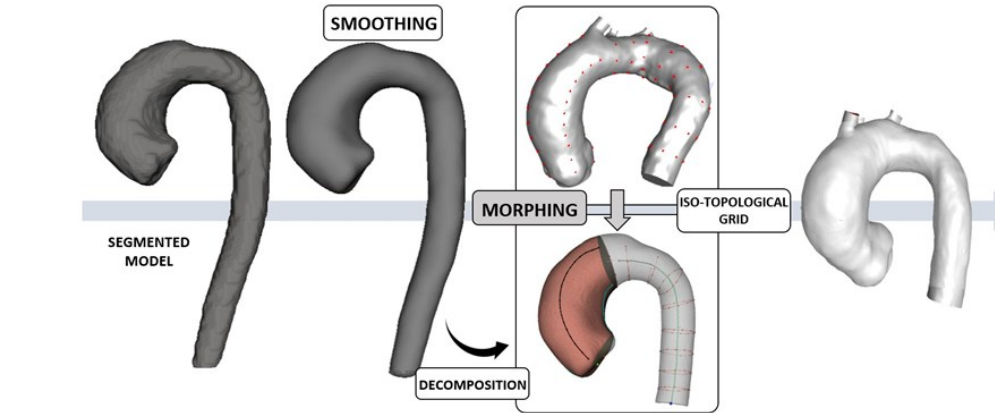
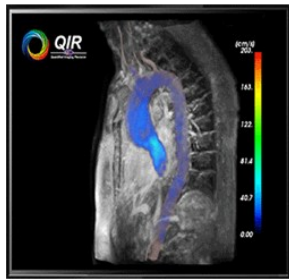
ONLINE PHASE





The offline phase

MRI 4D Flow



Based on principal component analysis (PCA)

Each shape $\tilde{M}_S^i$ can be built combining n_{SM} eigenvalues λ_j and n_{SM} eigenvectors $\mathbf{W}_j$

$$\tilde{M}_S^i = M_{S_{\text{mean}}} + \sum_{j=1}^{n_{SM}} c_j^i \sqrt{\lambda_j} \mathbf{W}_j$$

Automatic (3D U-net)
segmentation methods
developed by Marin-Castrillon
et al. [11]

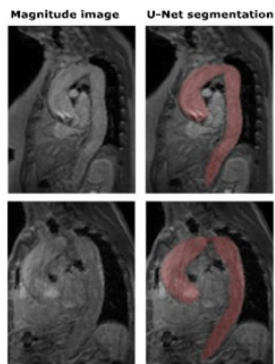
3D model

RBF Mesh
Morphing

Iso-topological
grid

Statistical Shape
Modeling

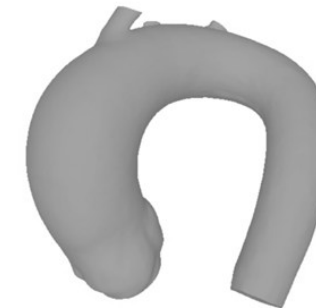
Parametric
3D model



$$s(\mathbf{x}) = \sum_{i=1}^N \gamma_i \varphi(\|\mathbf{x} - \mathbf{x}_{s_i}\|) + h(\mathbf{x})$$

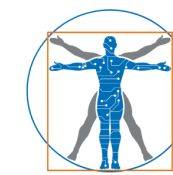
In the 3D space:

$$\mathbf{x}_{\text{node}_{\text{new}}} = \mathbf{x}_{\text{node}} + \begin{bmatrix} s_x(\mathbf{x}_{\text{node}}) \\ s_y(\mathbf{x}_{\text{node}}) \\ s_z(\mathbf{x}_{\text{node}}) \end{bmatrix}$$

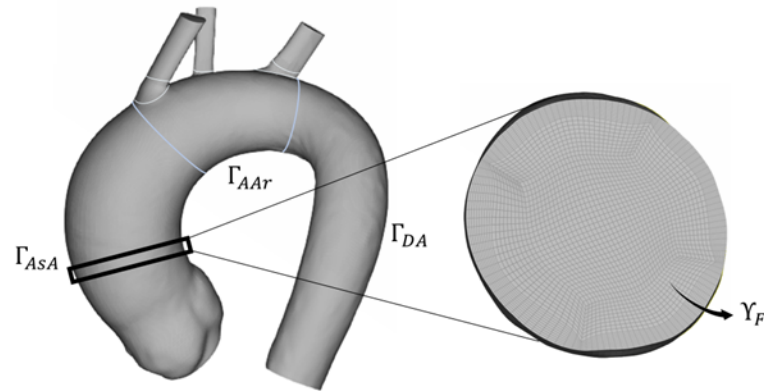


[11] Marin-Castrillon et al. *Magnetic Resonance Materials in Physics, Biology and Medicine* (2023): 1-14.

RBF Morph - www.rbf-morph.com



The offline phase

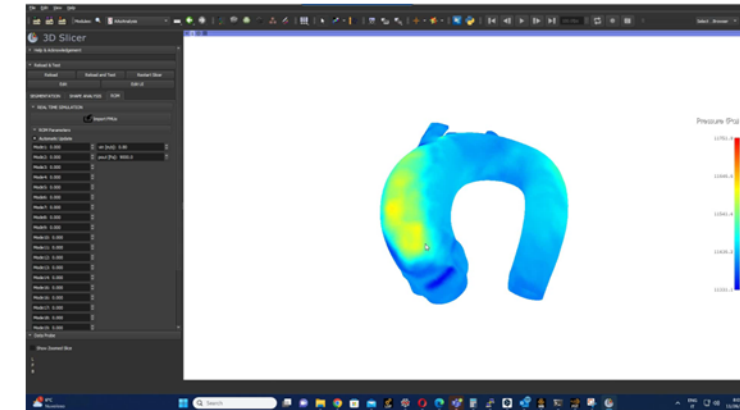


1) DECOMPOSITION

Proper orthogonal decomposition
(**POD**) techniques:

$$\Omega = U\Sigma V^T$$

$$\min_{\Phi} \|\Omega - \Phi\Phi^T\|^2$$



CFD Simulation using the
synthetic data created
through SSM

Set of learning
snapshots
(Wall pressure)

Model order reduction
techniques

Surrogate
Model

Surrogate model deployment

Navier-Stokes equations:

$$\mathbf{u} \cdot \nabla \mathbf{u} = -\frac{1}{\rho} \nabla p + \nu \nabla^2 \mathbf{u}, \text{ in } \gamma_F$$

$$\nabla \cdot \mathbf{u} = 0, \text{ in } \gamma_F$$

SIMPLE pressure-velocity coupling

Parameteric velocity **inlet** – pressure **outlet** BCs

2) INTERPOLATION

Genetic Aggregation Response Surface
(**GARS**) technique for the ROM interpolation

19

5

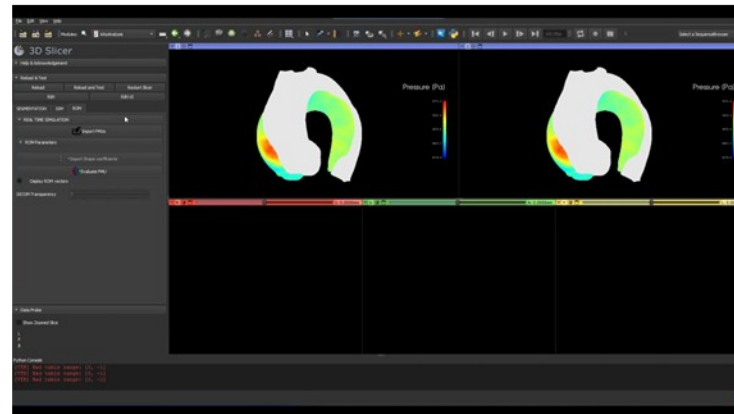
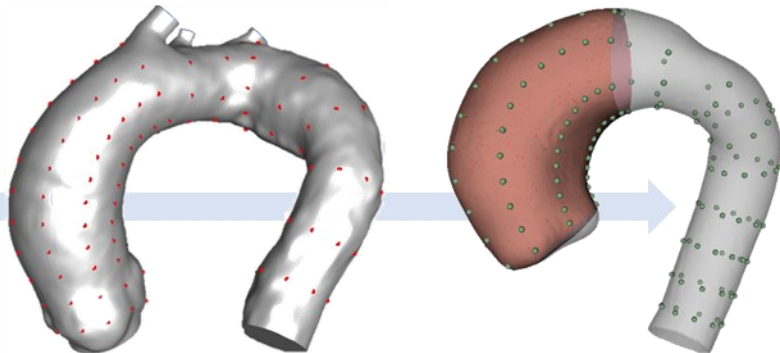
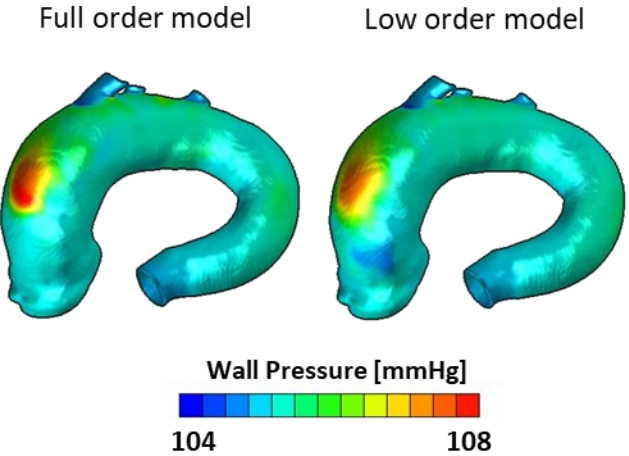
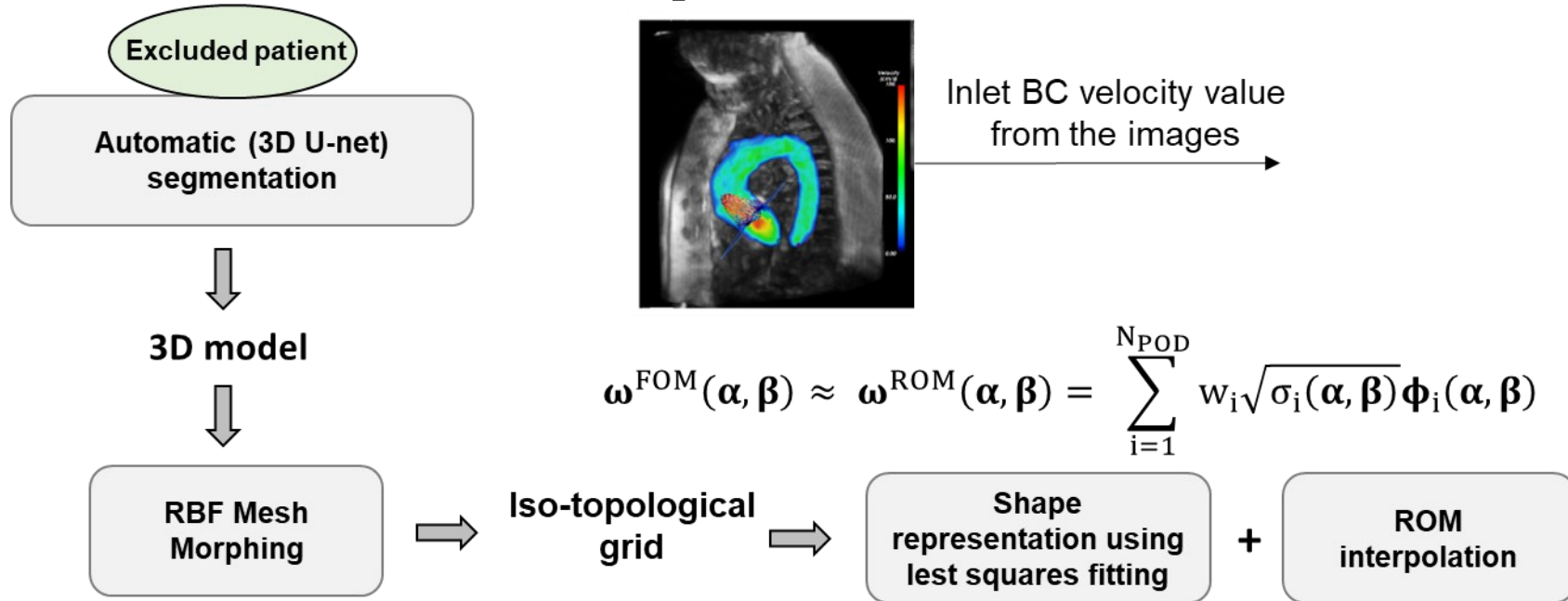
Geometrical parameters Physical parameters



FMU DEPLOYMENT
Model Exchange 2.0



The online phase

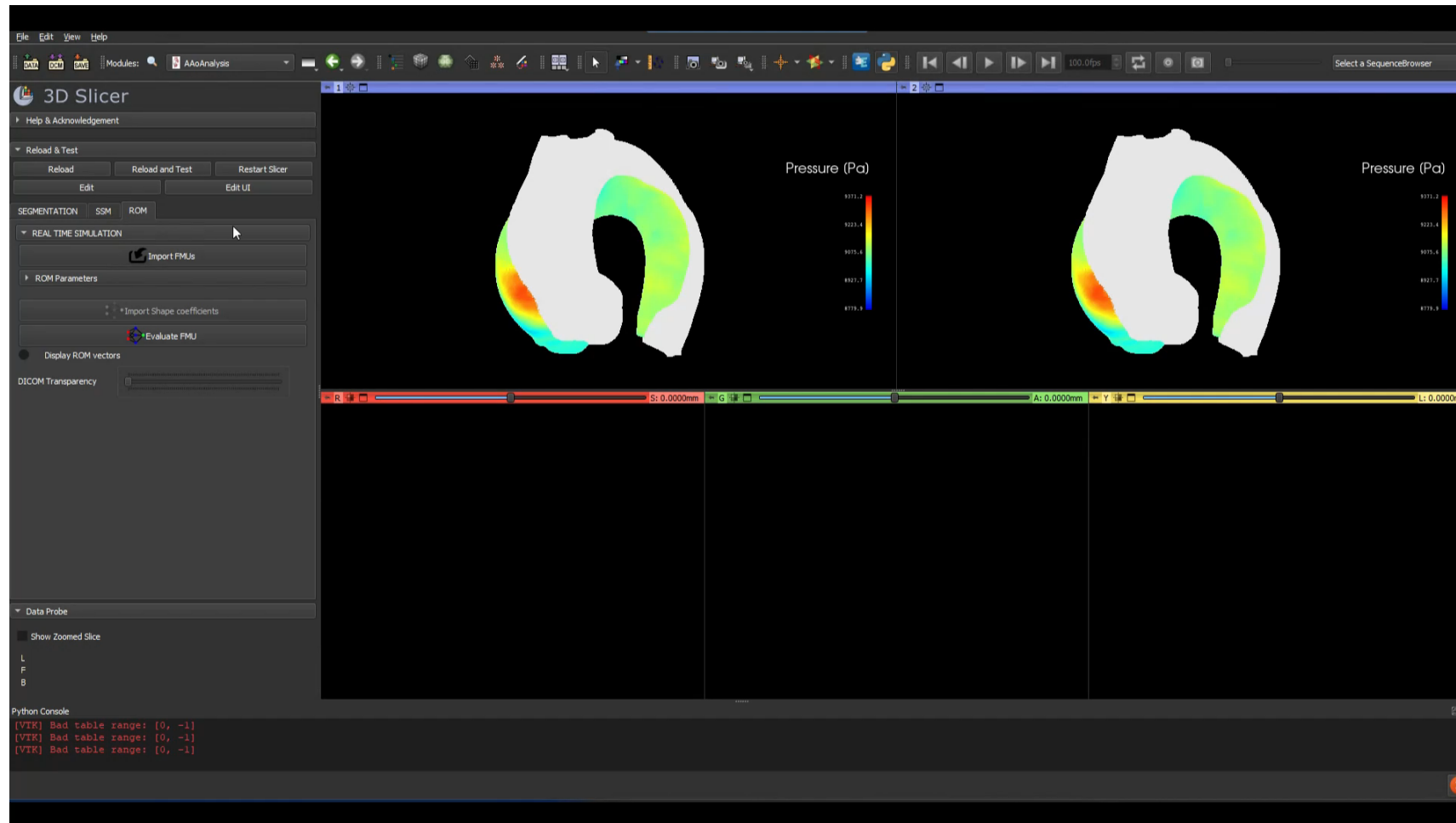


$$e_{\text{ROM}}^{\text{rel},i-\text{out}} = \frac{\|\omega_{i-\text{out}}^{\text{FOM}} - \omega_{i-\text{out}}^{\text{ROM}}\|}{\|\omega_{i-\text{out}}^{\text{ROM}}\|}$$

$$e_{\text{ROM}}^{\text{abs},i-\text{out}} = \max(\|\omega_{i-\text{out}}^{\text{FOM}} - \omega_{i-\text{out}}^{\text{ROM}}\|)$$



The online phase





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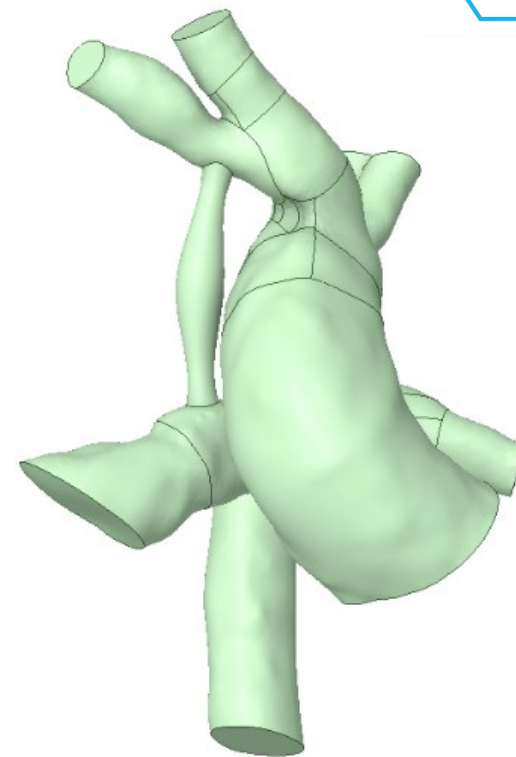
Support to shunting procedures

From Copernicus to ROMed2VR



Copernicus

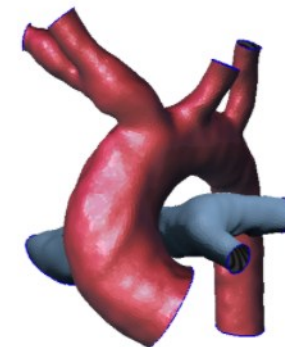
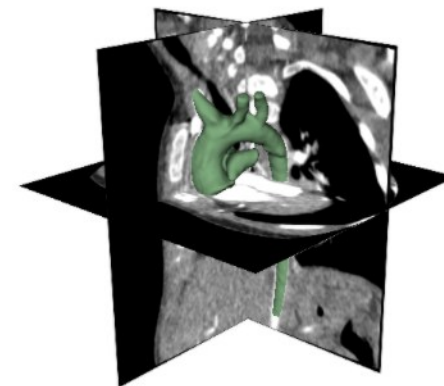
- Cloud-Based HPC Platform to Support Systemic-Pulmonary Shunting Procedures
- Congenital Heart Diseases (CHDs) = $\sim 1/3$ of all birth defects
- **Modified Blalock Taussig Shunt (mBTS)**
- Common palliative surgery for cyanotic CHD
- High risk: **over-shunting** & **shunt thrombosis** - significant mortality
- **Need:** better tools to support surgical planning & improve outcomes





Copernicus

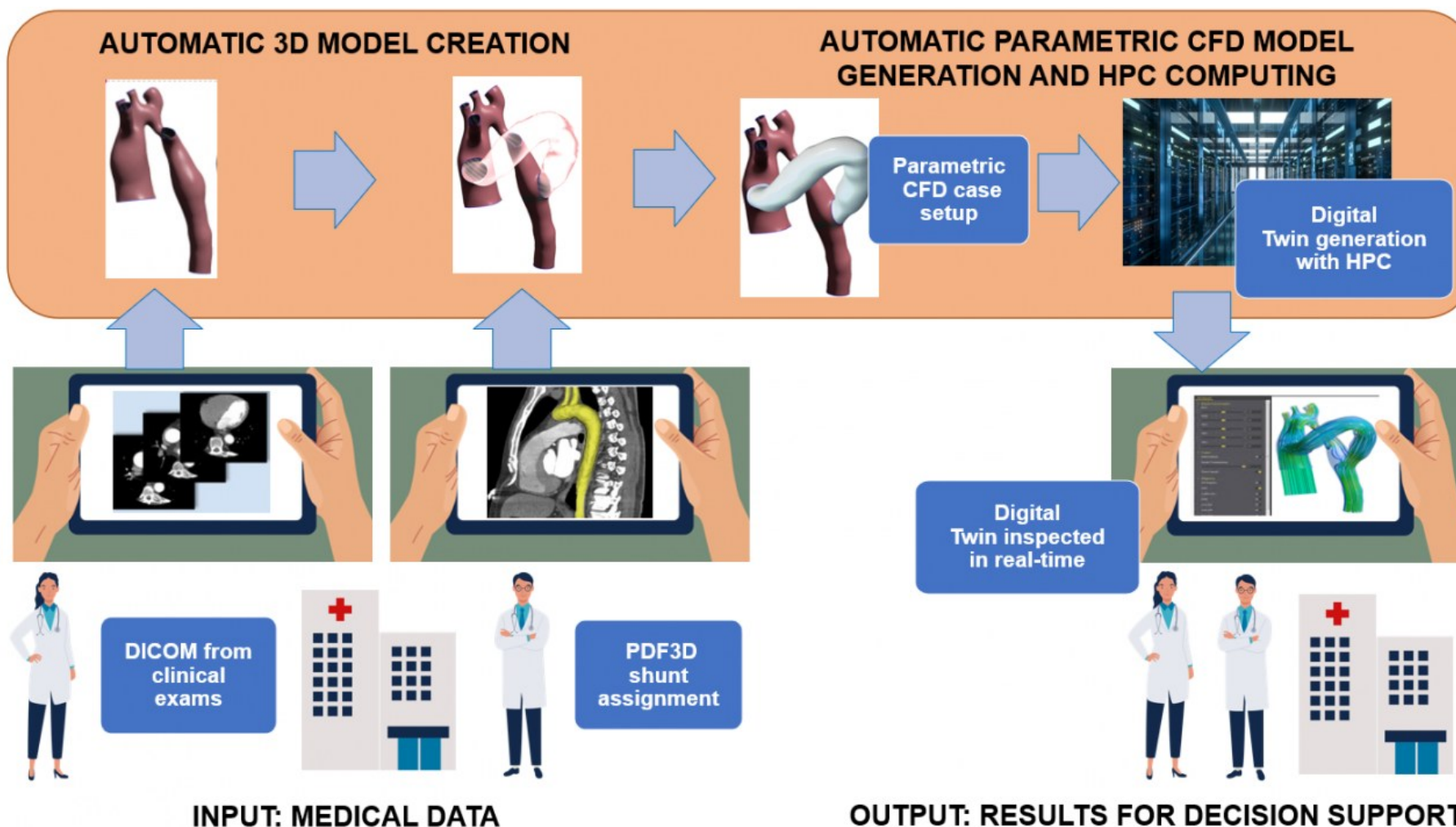
- **Patient-specific** digital twin (MDT) built via advanced **CFD simulations**
- Runs on cloud-based **HPC**: reliable & cost-efficient
- Reduced Order Model (ROM) of vascular district with **shunt parameterization**
- Interactive web interface for medical staff to explore scenarios
- Impact: Affordable **decision-support** tool, safer, tailored mBTS interventions



Medical Digital Twin Copernicus



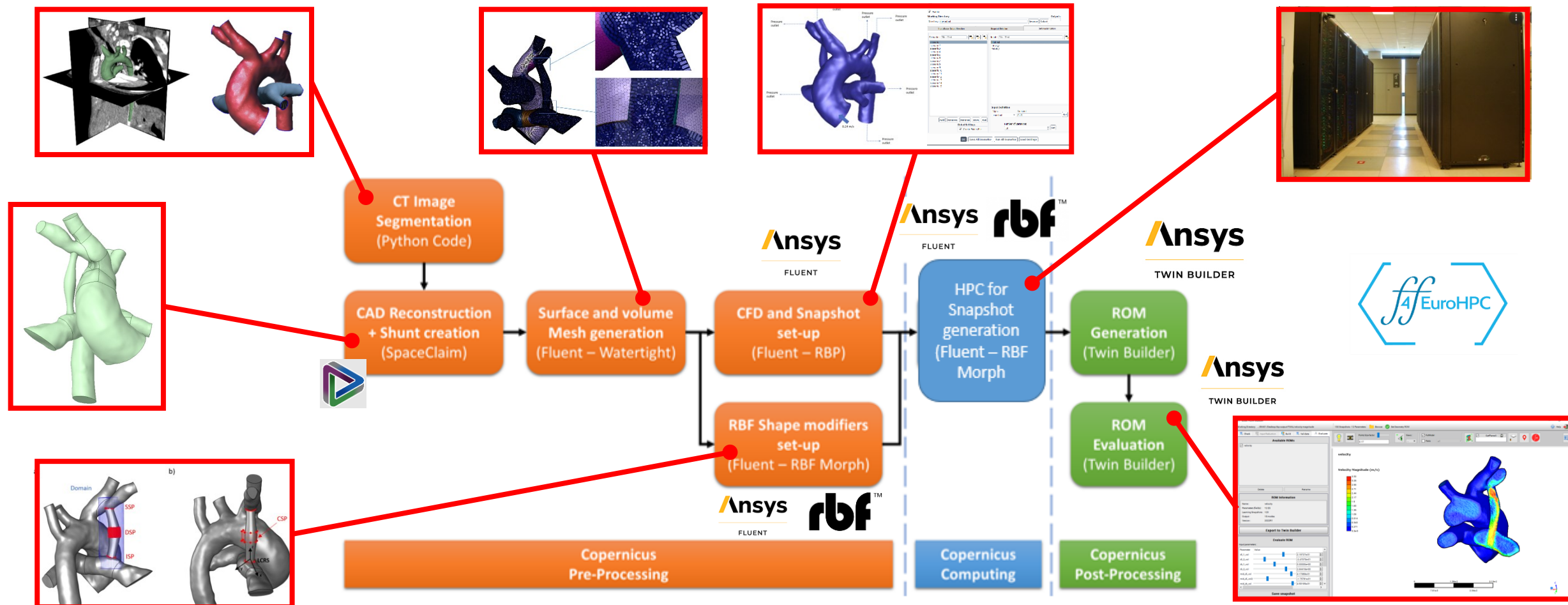
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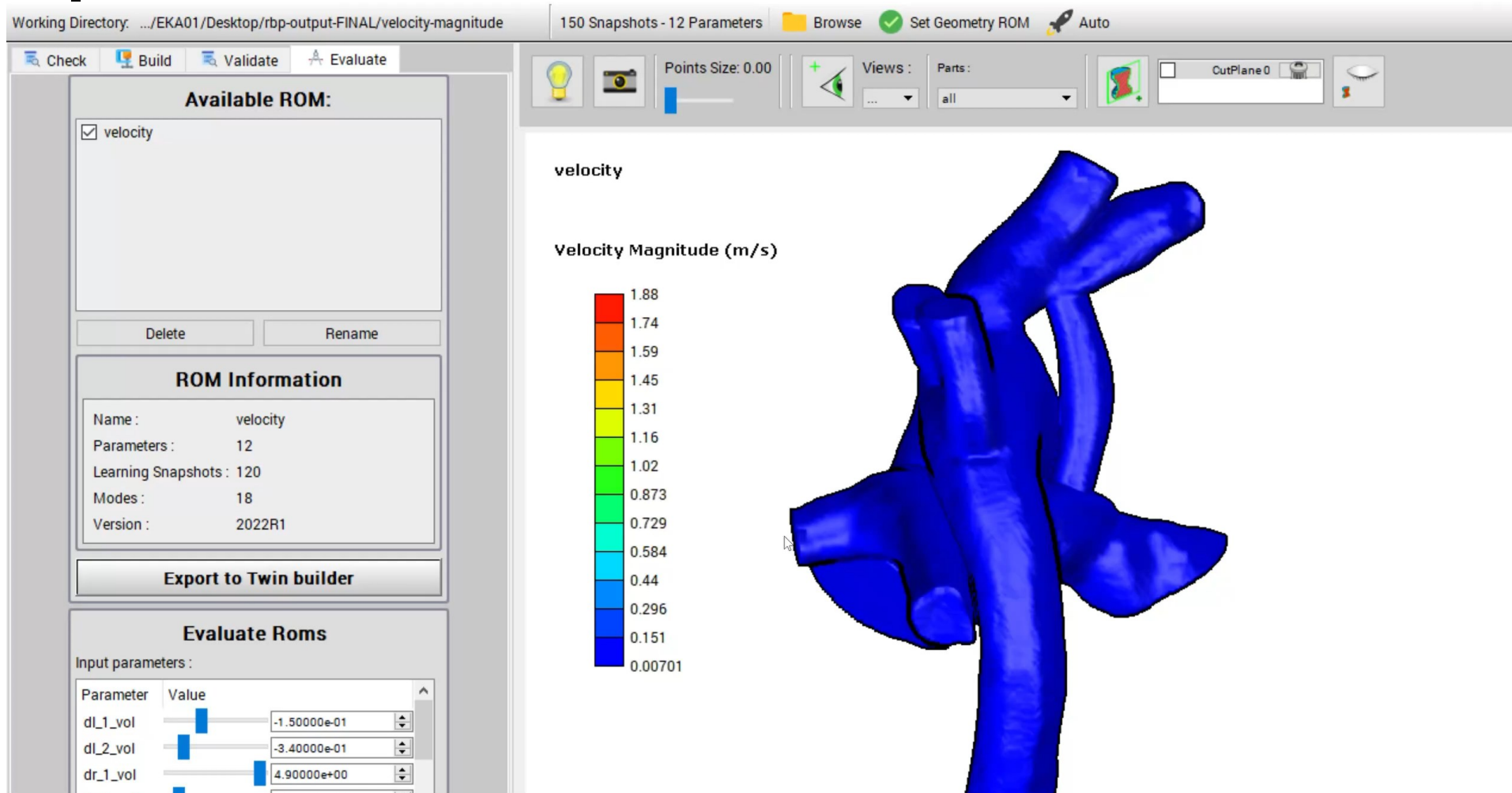
Medical Digital Twin Copernicus



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Medical Digital Twin Copernicus



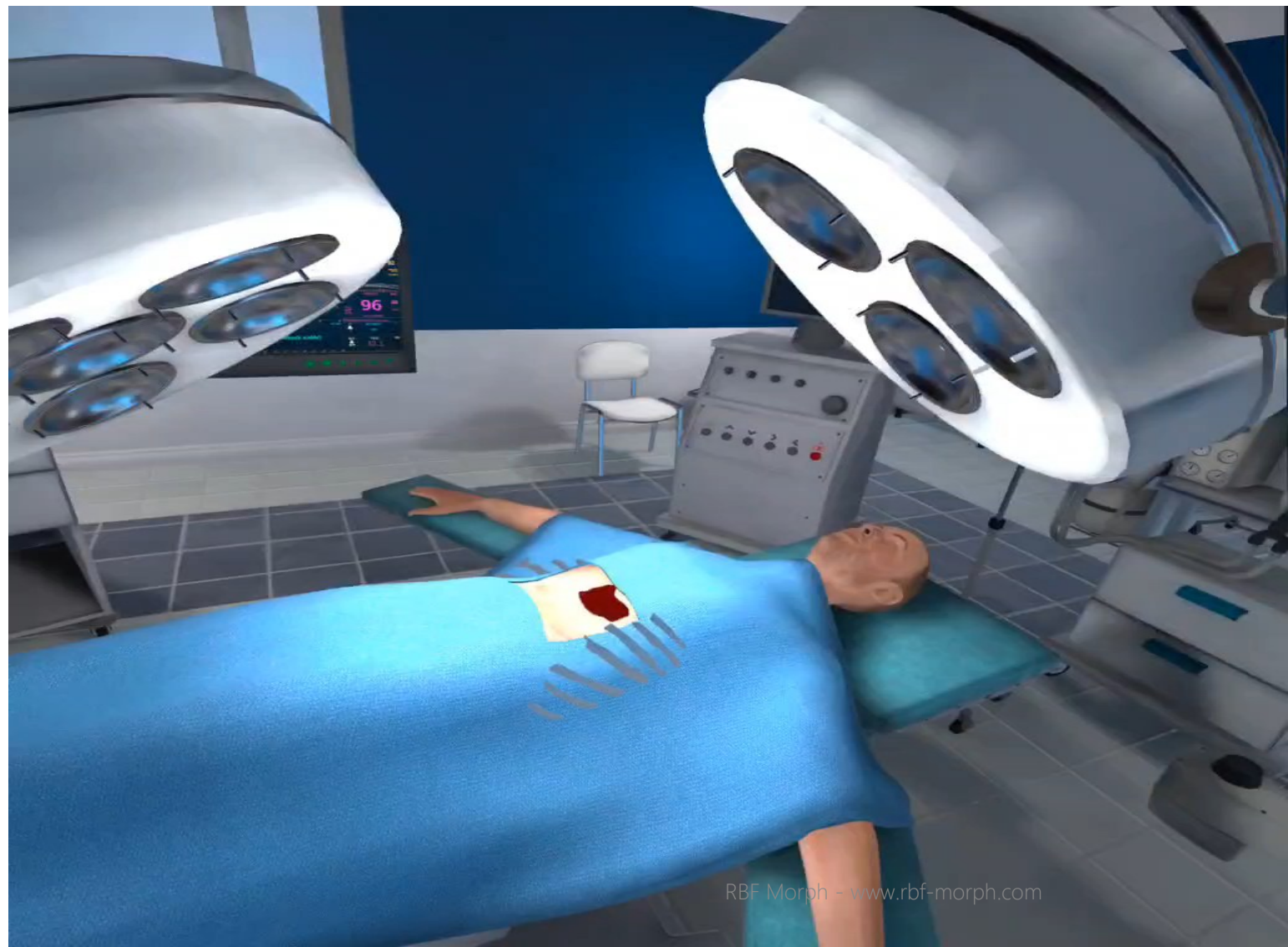
Next step?

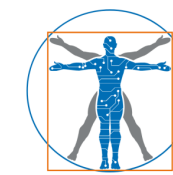
A complete solution to deliver interactive digital twins with AR/VR custom UI



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- FMU are translated to ARM
- Meta Quest 3
- Apple Vision Pro (very soon!)
- Input parameters are controlled by hands

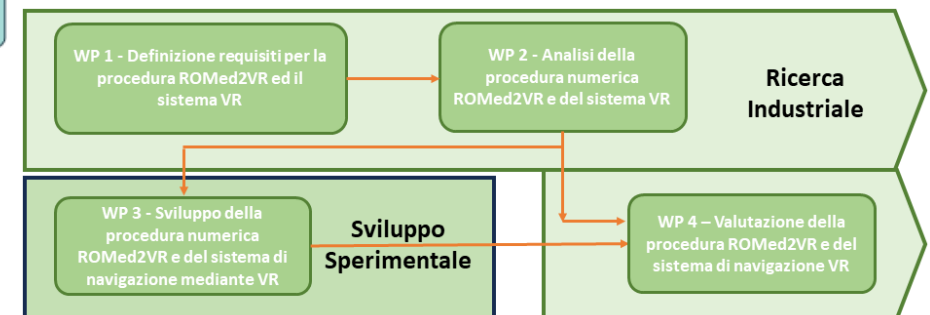
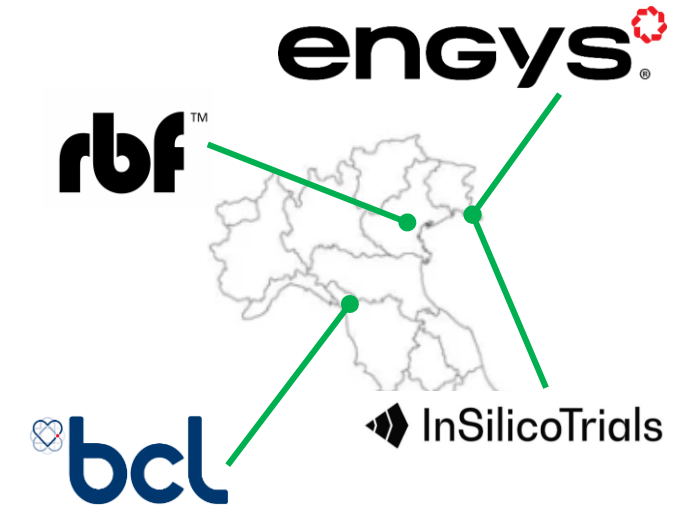
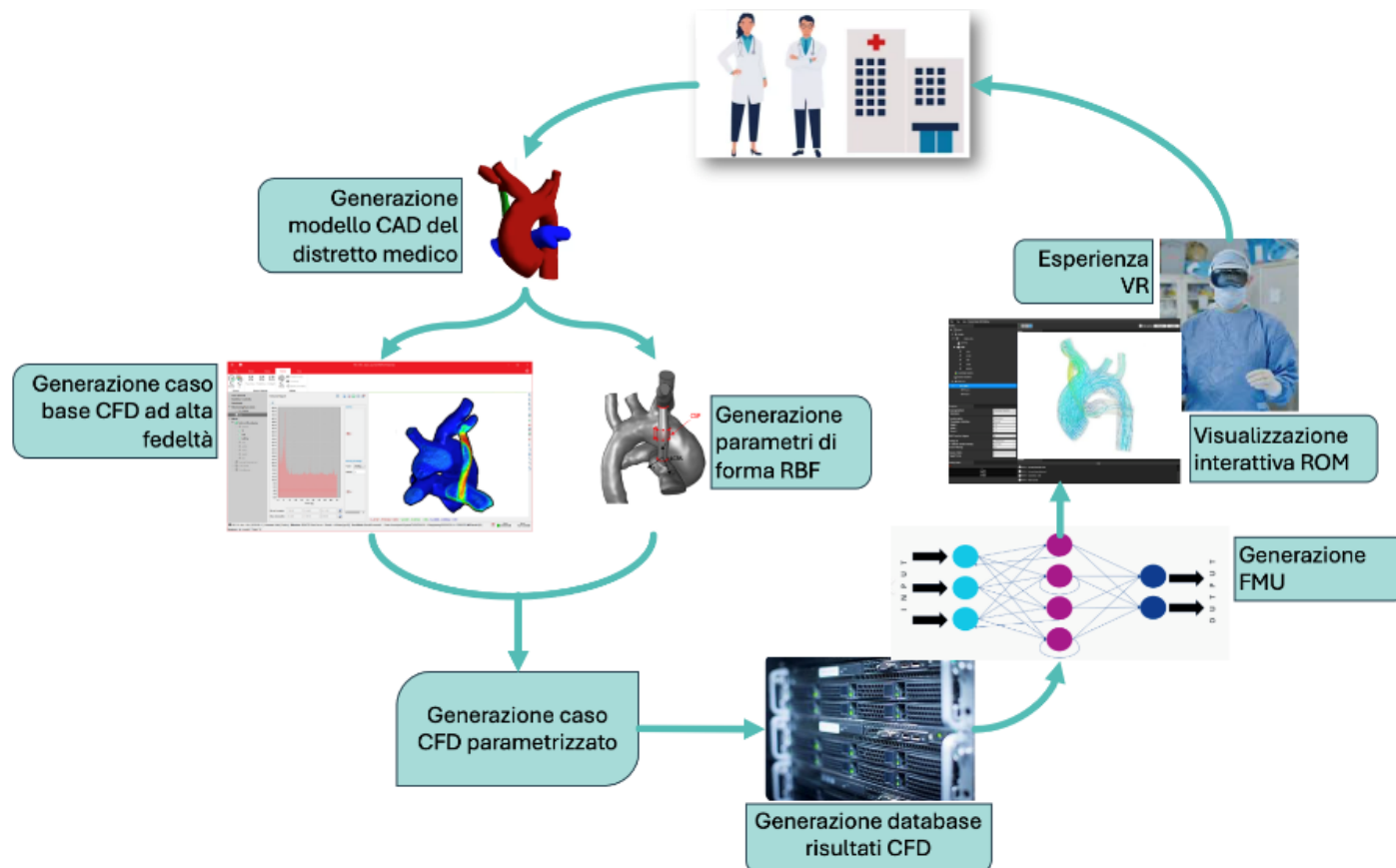




ROMed2VR

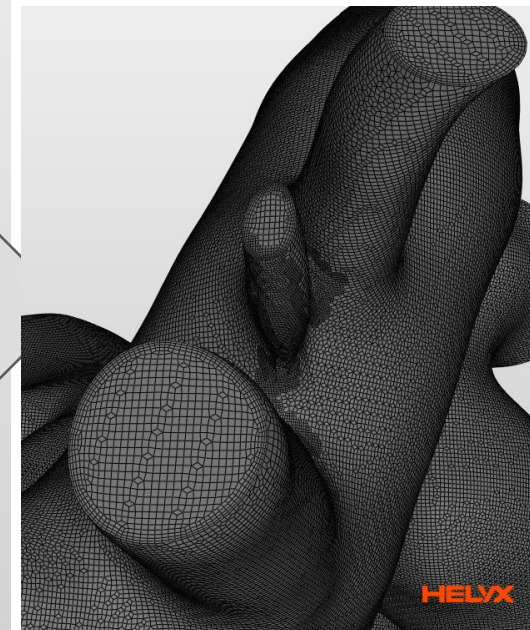
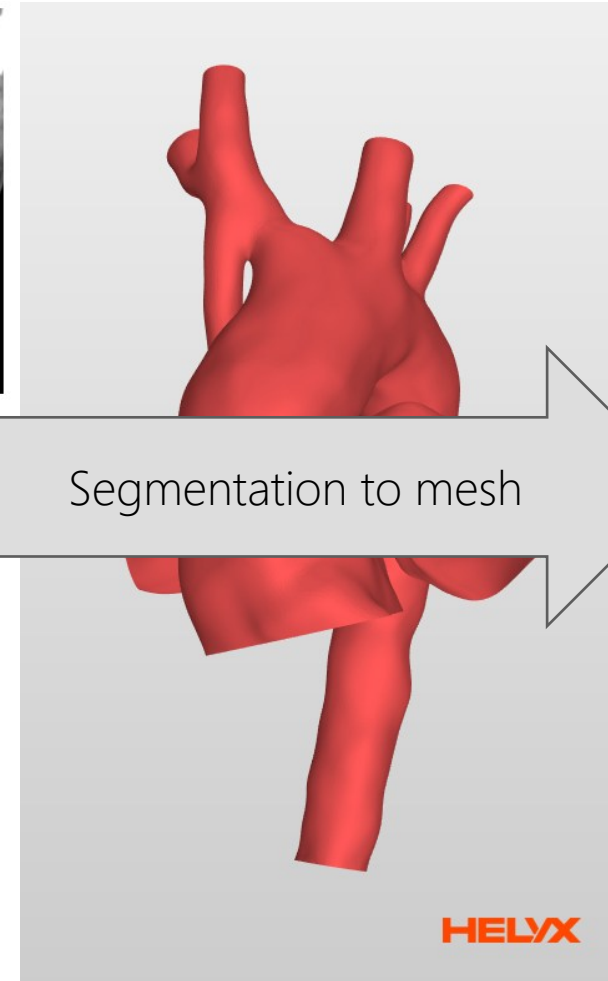
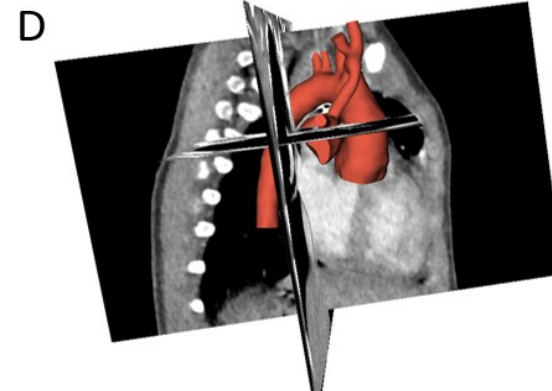
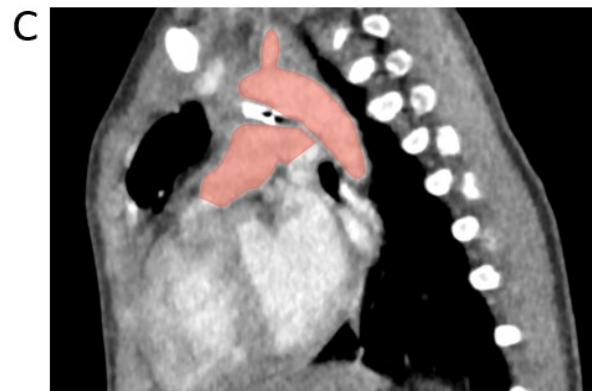
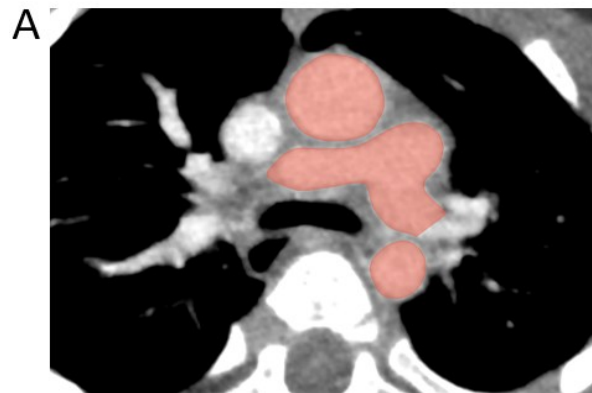
i NEST

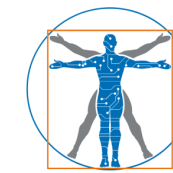
Interconnected
Nord-Est Innovation
Ecosystem





ROMed2VR

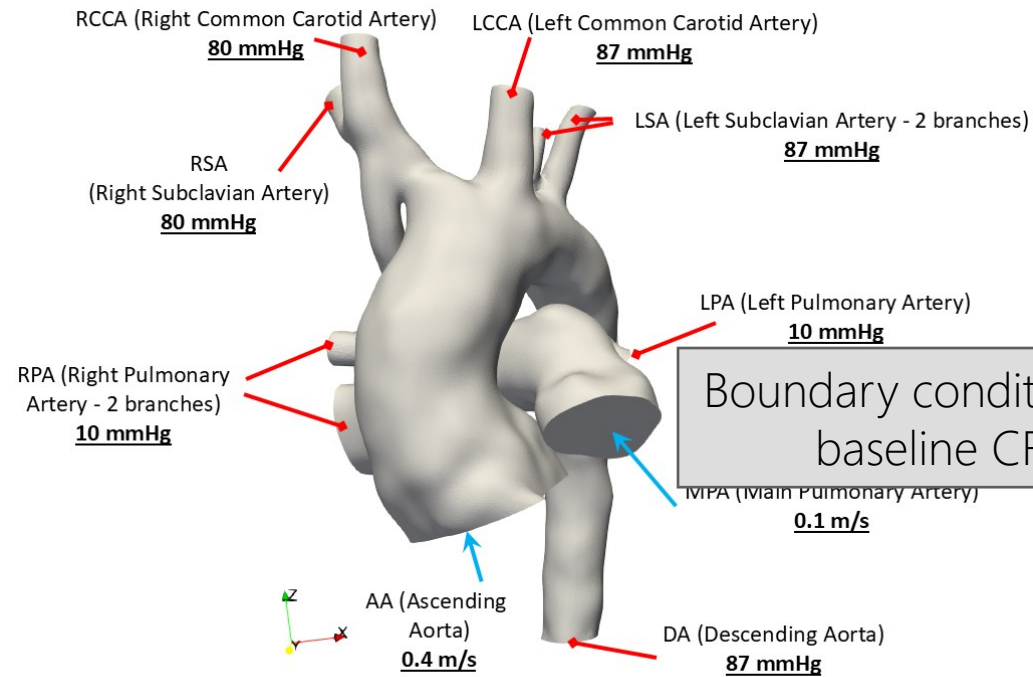




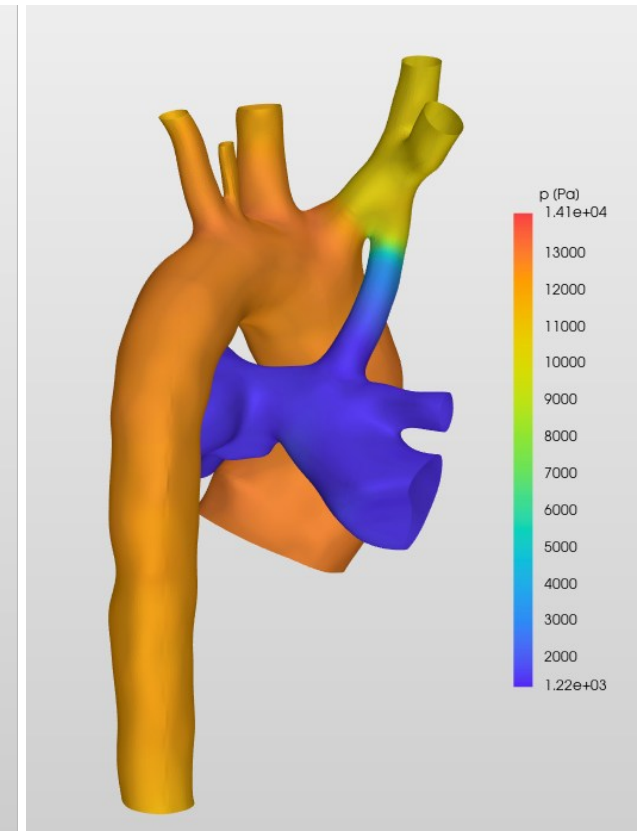
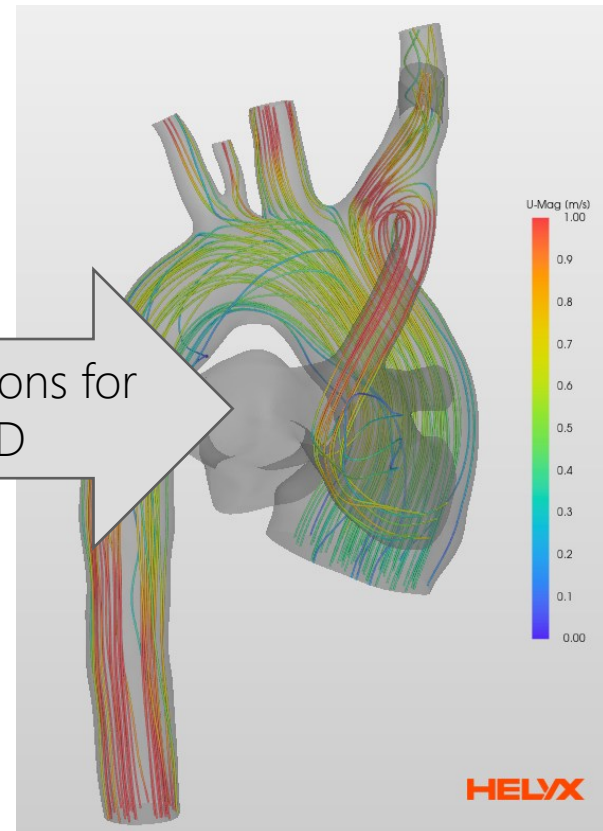
ROMed2VR

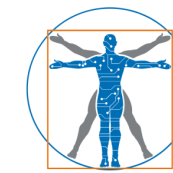


Interconnected
Nord-Est Innovation
Ecosystem

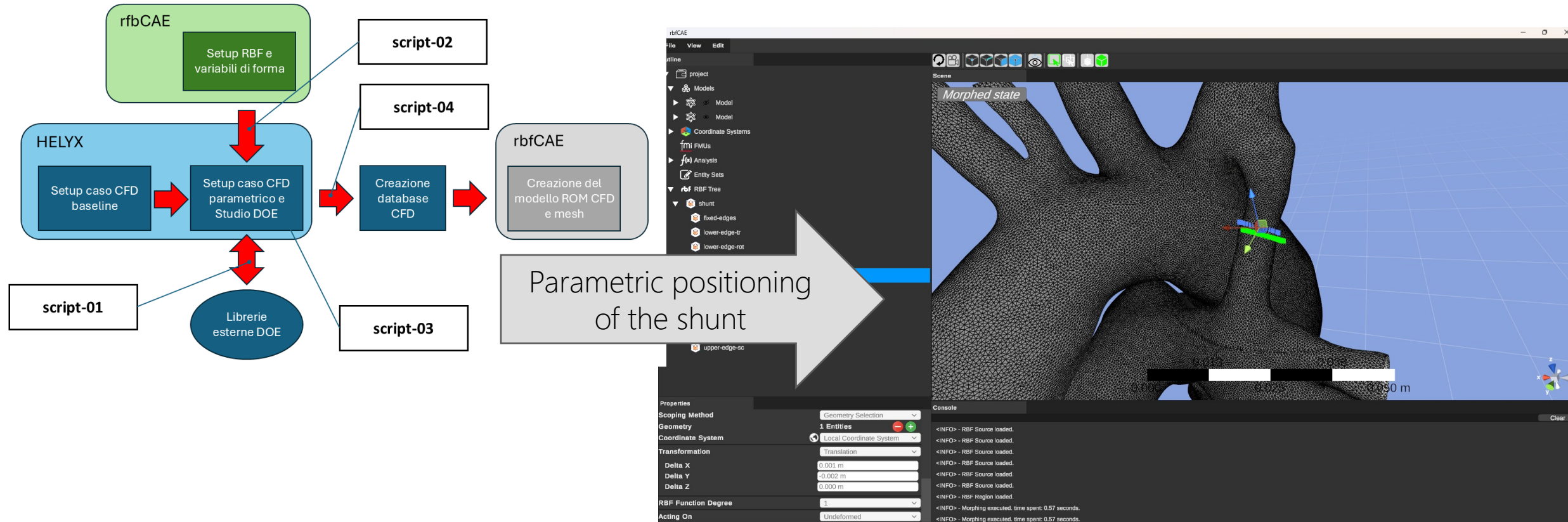


Boundary conditions for
baseline CFD





ROMed2VR

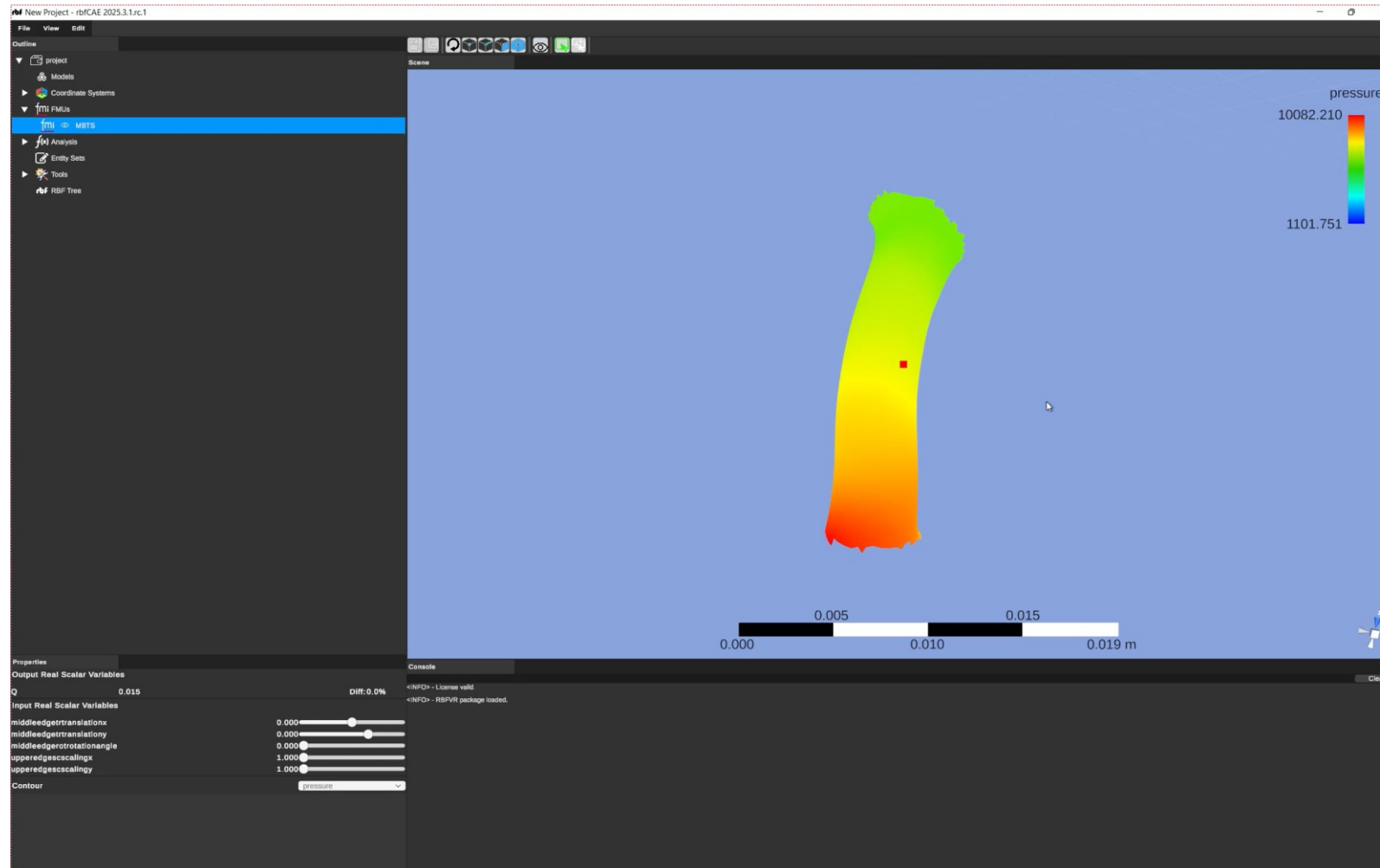




ROMed2VR



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Ecosystem



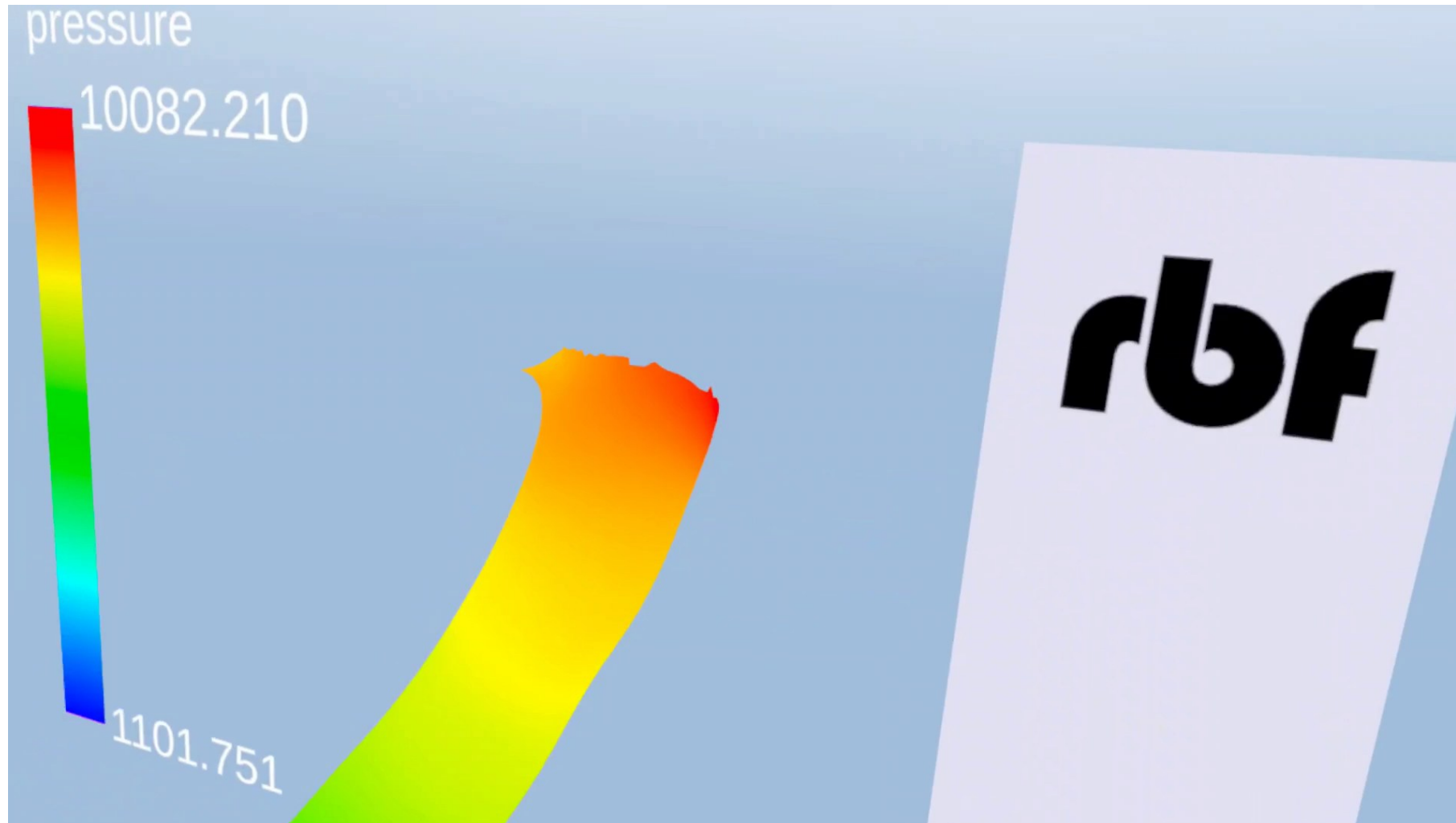


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i NEST

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Ecosystem





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RBF Morph technologies

A complete solution for Medical Digital Twins

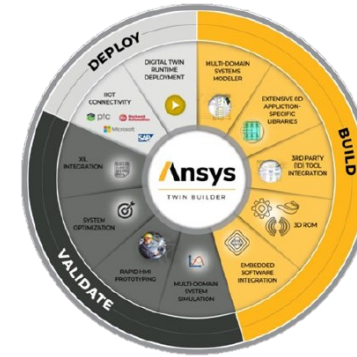


RBF Morph - www.rbf-morph.com



Ansys RBF Morph

- An RBF mesh morphing solution fully embedded in **Ansys**
 - **Ansys RBF Morph Fluids** – an Add On for Fluent
 - **Ansys RBF Morph Structures** – an ACT App for Mechanical
- Full integration with **optiSLang** and **Twin Builder**
- Support for **LS-DYNA** and **APDL**



Add-On Packages

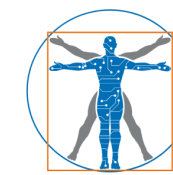
Ansys RBF Morph



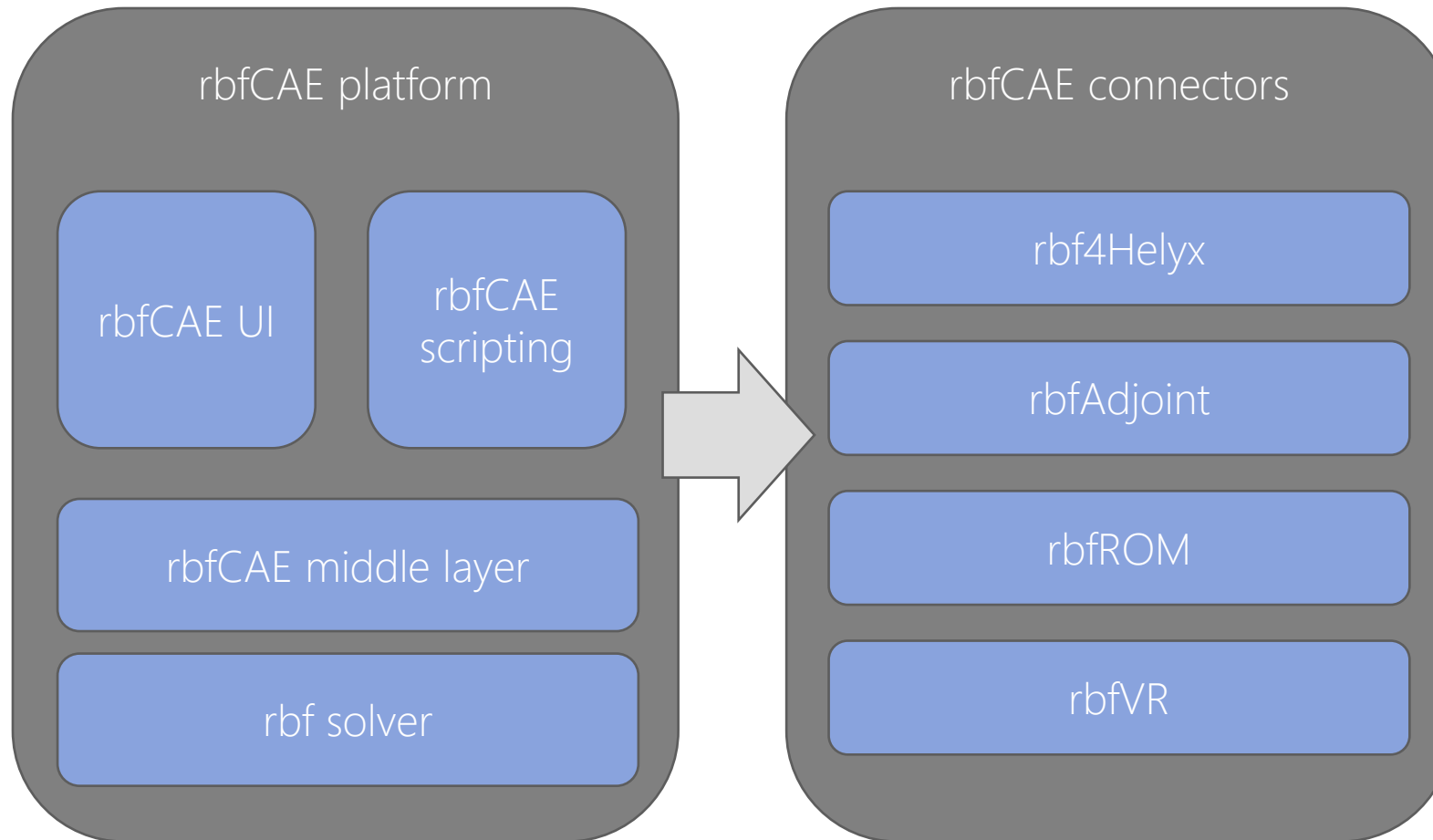
↓ Fluids

↓ Structures

Ansys
part of **SYNOPSYS®**



rbfCAE solution



- Released in 2024
- Read in **STL, STEP**
- **Unity - OpenCascade**
- Solver independent process that supports **many mesh formats**
- **Scriptable** via python



Conclusions

- Interactive Digital Twins? **Yes!**
- We can deploy fast interactive ROM on VR and on custom dashboards
- We use RBF both for the geometrical intelligence and both for the AI inference
- Multiple workflow are supported: a variety of CAE software can be combined to mesh morphing to generate synthetic datasets
- The approach works both for parametric cases (shapes are varied according to specific actions) both for SSM (shapes are collected from a cohort of data)



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Association for Predictive Medicine

Many thanks for your attention!

marco.biancolini@rbf-morph.com



linkedin.com/company/rbf-morph



youtube.com/user/RbfMorph



rbf-morph.com