

Structural Optimization of Internal Combustion Engines Using RBF Mesh Morphing

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Founder of RBF Morph srl



Agenda

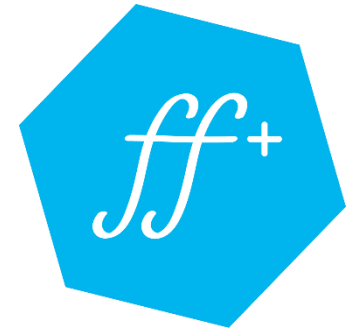
- About us – past and running projects
- Radial Basis Functions – Data Science and Geometrical Intelligence
- Parameter-based and parameter-free shape optimisation
- An industrial example: Internal Combustion Engine Components Fatigue Assessment
- Digital Engineering Applications
- Conclusions



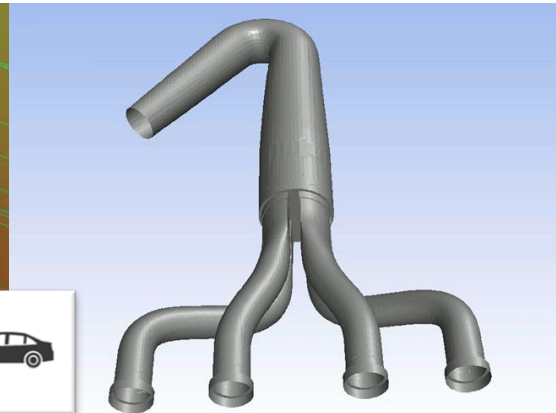
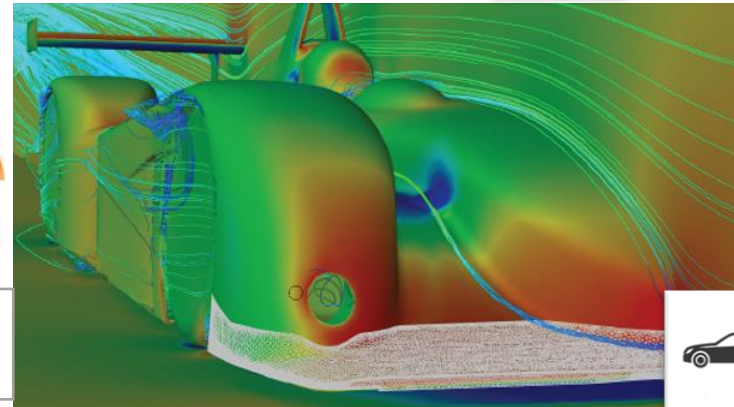
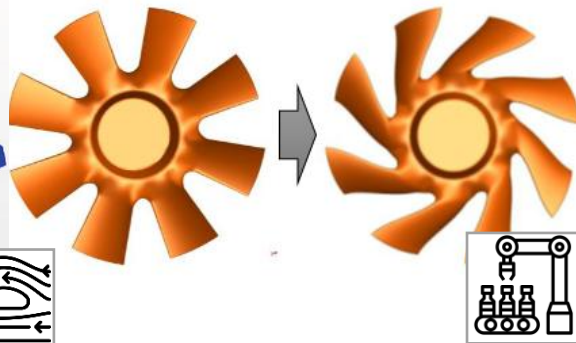
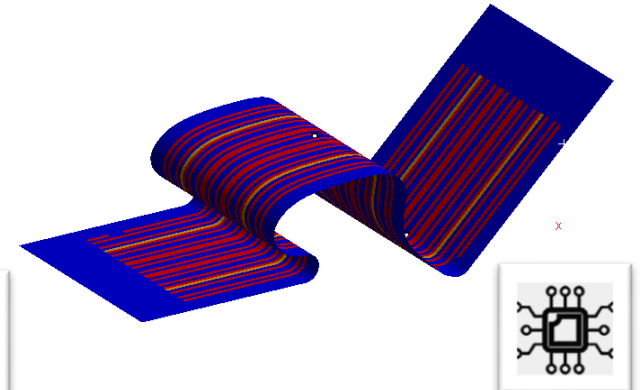
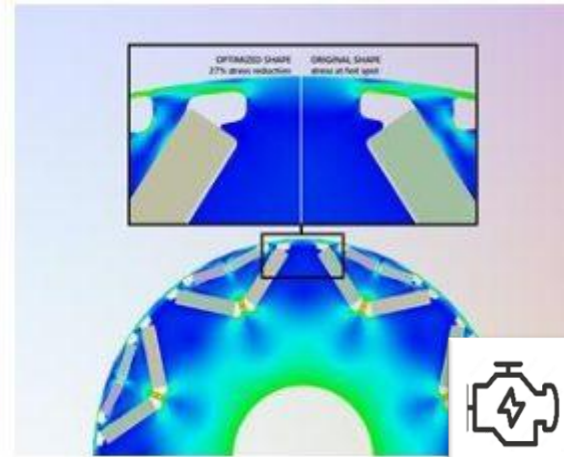
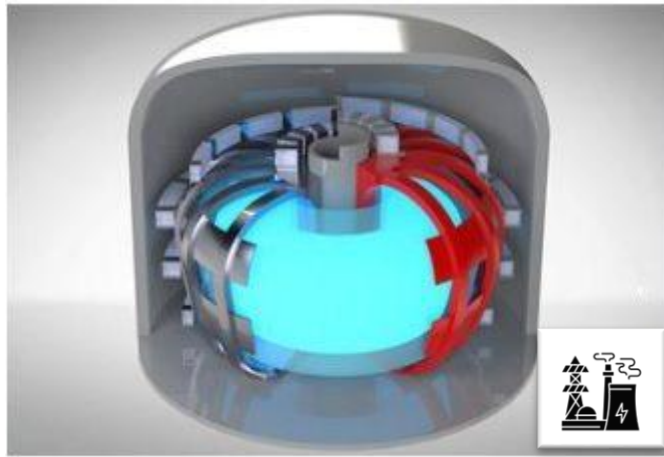
EU-funded research projects 2013-2025



Funded by
the European Union



Research and Industrial sectors



Radial Basis Functions

Data Science and Geometrical Intelligence

Radial Basis Functions (RBF) in a nutshell

source points

$$s(\mathbf{x}) = \sum_{i=1}^N \gamma_i \cdot \underbrace{\varphi(\|\mathbf{x} - \mathbf{x}_{k_i}\|)}_{\text{radial basis}} + \underbrace{h(\mathbf{x})}_{\text{polynomial}}$$

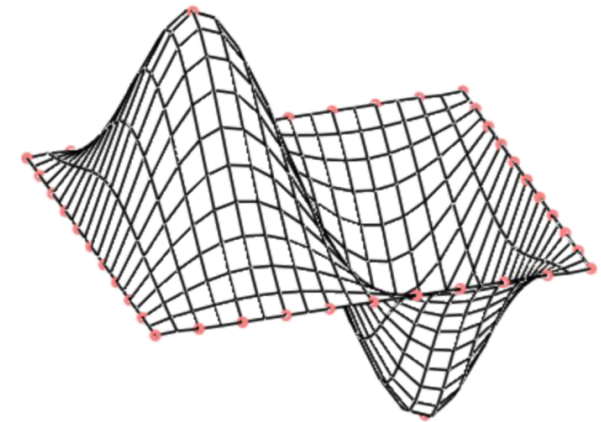
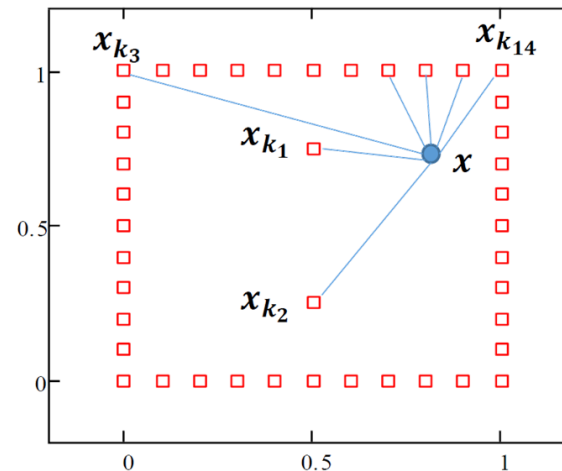
weight

e.g. $h(\mathbf{x}) = \beta_1 + \beta_2 x + \beta_3 y + \beta_4 z$

shift of the target point to the i-th data site

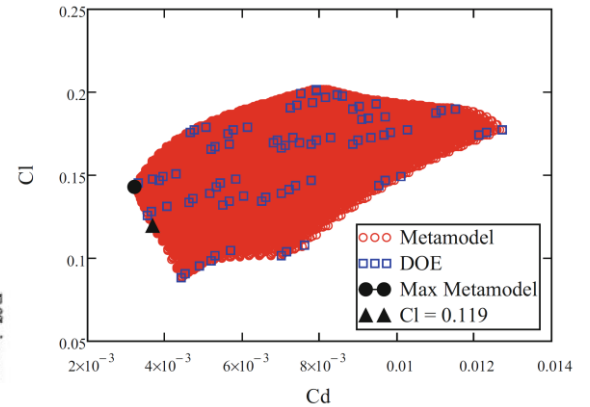
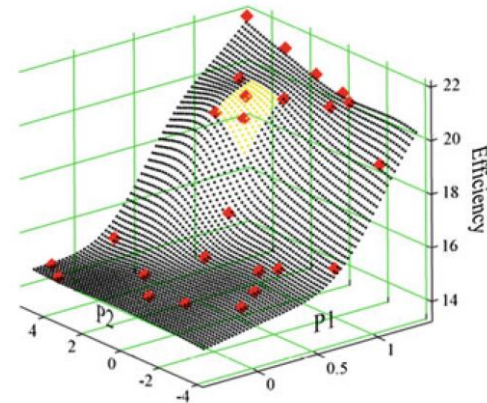
RBF	$\varphi(r)$
Spline type (Rn)	$r^n, n \text{ odd}$
Thin plate spline	$r^n \log(r) \text{ } n \text{ even}$
Multiquadratic (MQ)	$\sqrt{1 + r^2}$

RBF are a very powerful mathematical tool able to interpolate **everywhere** in the \mathbb{R}^n space a function given at scattered **source points**



Interpolators in multi-dimensional spaces

- **Data science** problems
 - Inference $\mathbb{R}^n \Rightarrow \mathbb{R}^m$
 - Gaussian RBF is recognized as the "RBF neural network"
 - Useful for **surrogates** in **optimisation**
- 3D space manipulation (shape deformation, data mapping)
 - Field manipulation is a key enabler for **geometric intelligence**
 - Mapping is a key enabler for multi-physics and as a "morphing extender"

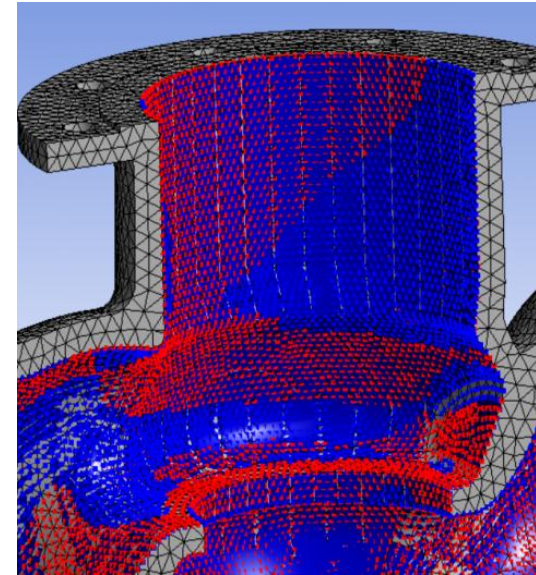


Shape optimisation

Parameter-based and parameter-free workflows

RBF Mesh Morphing

- We adopt **Radial Basis Functions** (RBF) to drive mesh morphing (smoothing) from a list of source points and their displacements
 - Surface shape changes
 - Volume mesh smoothing
- RBF are recognized to be one of the **best mathematical tool** for mesh morphing



Digital Engineering Day Roma

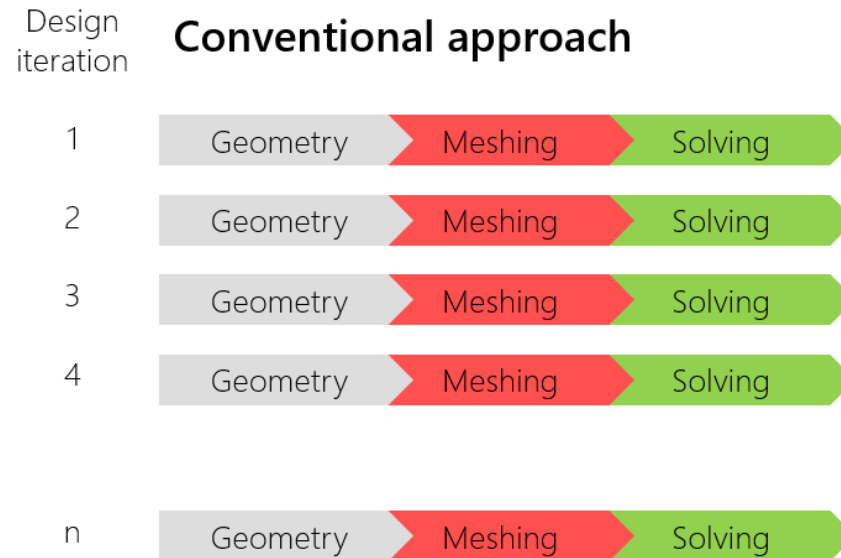
Simulazione numerica: il motore dell'innovazione digitale



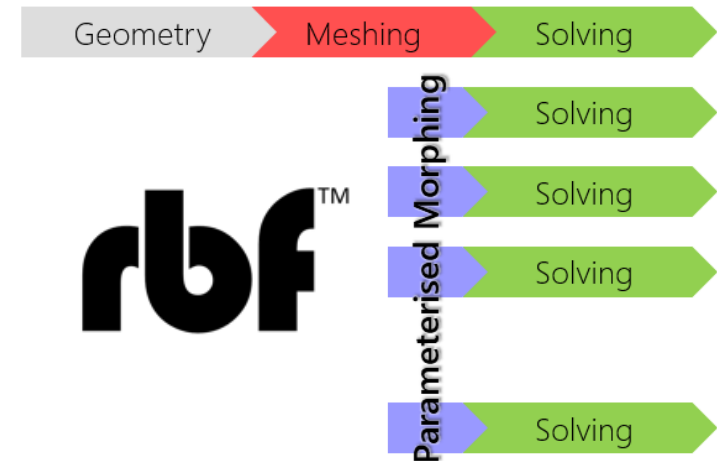
$$\begin{cases} s_x(\mathbf{x}) = \sum_{i=1}^N \gamma_i^x \varphi(\|\mathbf{x} - \mathbf{x}_{s_i}\|) \\ s_y(\mathbf{x}) = \sum_{i=1}^N \gamma_i^y \varphi(\|\mathbf{x} - \mathbf{x}_{s_i}\|) \\ s_z(\mathbf{x}) = \sum_{i=1}^N \gamma_i^z \varphi(\|\mathbf{x} - \mathbf{x}_{s_i}\|) \end{cases}$$

Parameter-based shape optimization

- Morphing is a **key enabler** for optimization and Digital Twins
- The turnaround time of the optimization is usually **reduced by a factor five** (weeks becomes days)

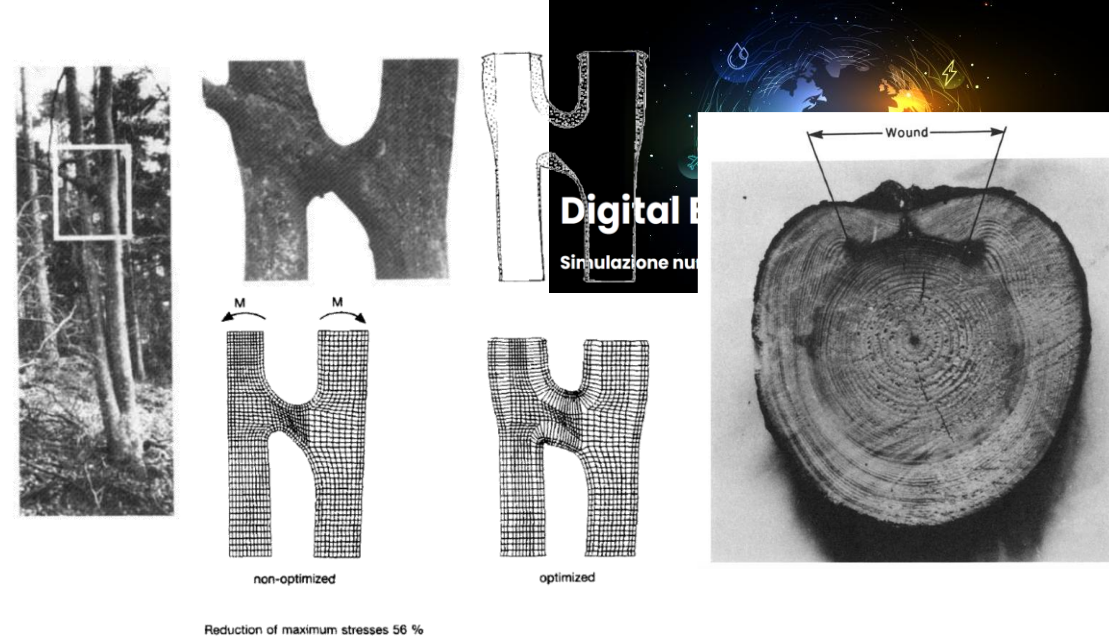


RBF's morphing approach

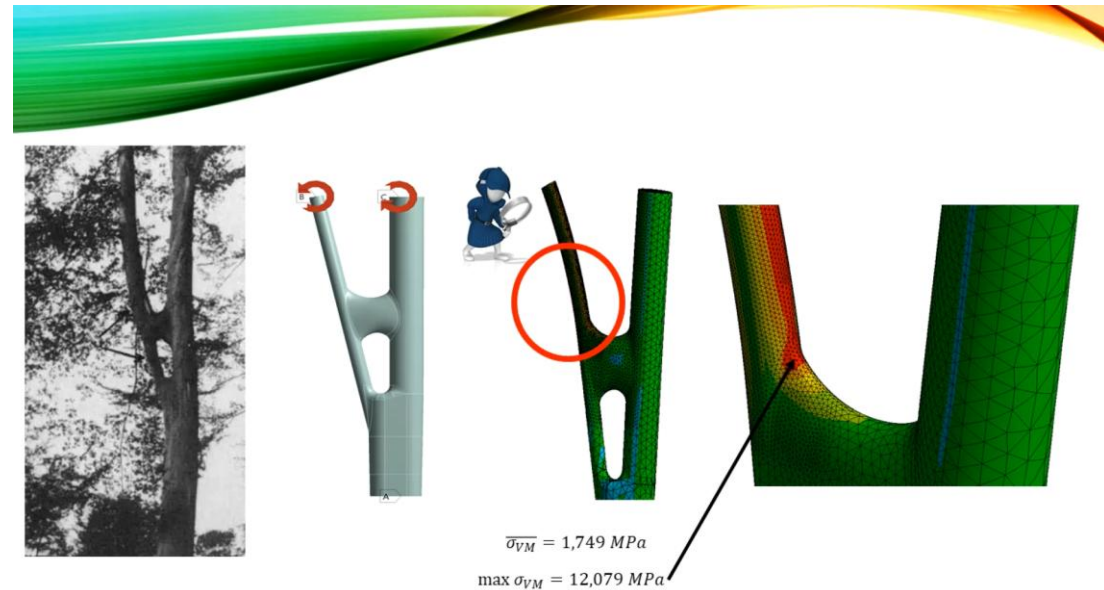


BGM Background

- BGM approach is based on the observation that **biological** structures growth is driven by **local** level of **stress**.
- Bones and trees' trunks are able to **adapt the shape** to mitigate the stress level due to external loads.
- The process is driven by stress **value** at **surfaces**. Material can be **added** or **removed** according to local values.
- Was proposed by Mattheck & Burkhardt in 1990



Reduction of maximum stresses 56 %



Parameter-free shape optimization

- The BGM idea is that surface growth can be expressed as a **linear law** with respect to a given threshold value:

$$\dot{\varepsilon} = k(\sigma_{Mises} - \sigma_{ref})$$

- Waldman and Heller refined this first approach proposing a **multi peak** one:

$$d_i^j = \left(\frac{\sigma_i^j - \sigma_i^{th}}{\sigma_i^{th}} \right) \cdot s \cdot c, \quad \sigma_i^{th} = \max(\sigma_i^j) \text{ if } \sigma_i^j > 0 \quad \text{or} \quad \sigma_i^{th} = \min(\sigma_i^j) \text{ if } \sigma_i^j < 0$$

- A different implementation is present and different **stress types** can be used to modify the surface shape:

$$S_{node} = \frac{\sigma_{node} - \sigma_{th}}{\sigma_{max} - \sigma_{min}} \cdot d$$

An industrial example

Internal Combustion Engine Components Fatigue Assessment

Collaboration Context

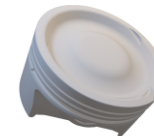
- RBF Morph, Piaggio and University of Rome Tor Vergata supported by **Ansys**
- **Topic:** Structural optimization of a Piaggio 4-stroke engine **connecting rod & piston**
- **Methods:** Parametric mesh morphing + BGM Method within an Ansys-based workflow
- **Outcomes:** A **team project** for the course *Tecnica delle Costruzioni Meccaniche (Advanced Machine Design)* and a **bachelor degree thesis**



LAUREA TRIENNALE IN
INGEGNERIA MECCANICA

Ottimizzazione strutturale della biella di
un motore a quattro tempi: dalla
simulazione FEM ad alta fedeltà
all'intelligenza artificiale

Relatore:
Prof. Marco Evangelos Biancolini
Correlatore:
Ing. Emanuele Di Meo



**Ottimizzazione e analisi a fatica del
pistone di un motore Piaggio 150cc**

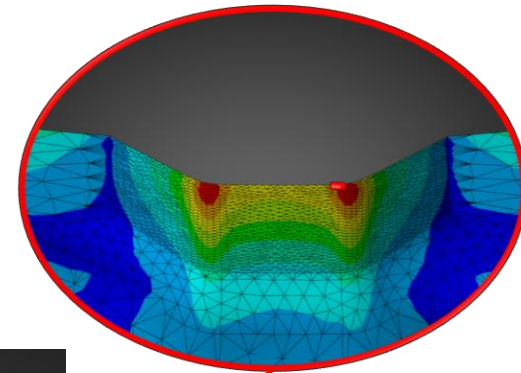
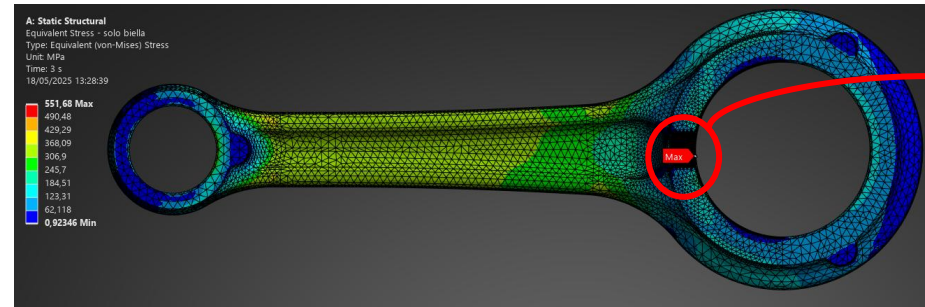
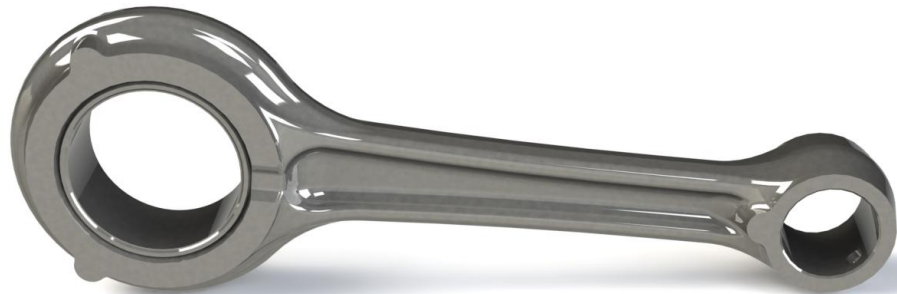


Corso di Tecnica delle Costruzioni Meccaniche
Barbagelata Filippo, Cafolla Fabiano, De Iacovo Luna, Jral Marco, Marica Gaia
Prof. Ing. Marco Evangelos Biancolini

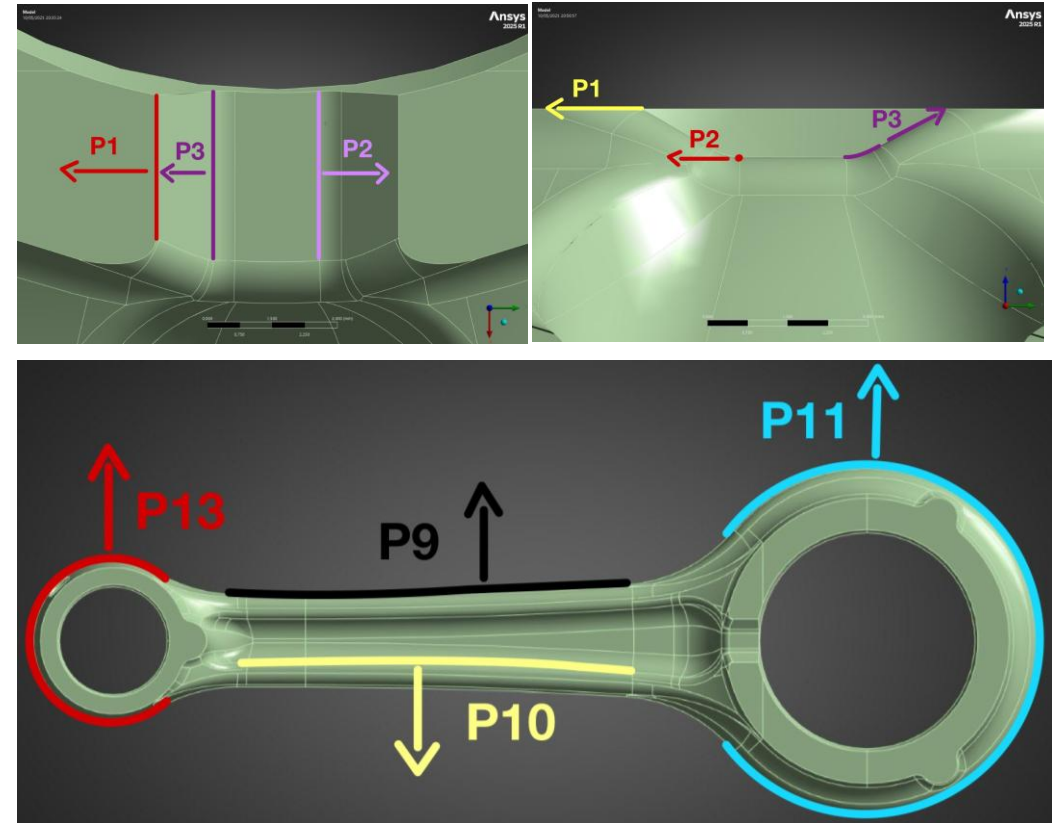
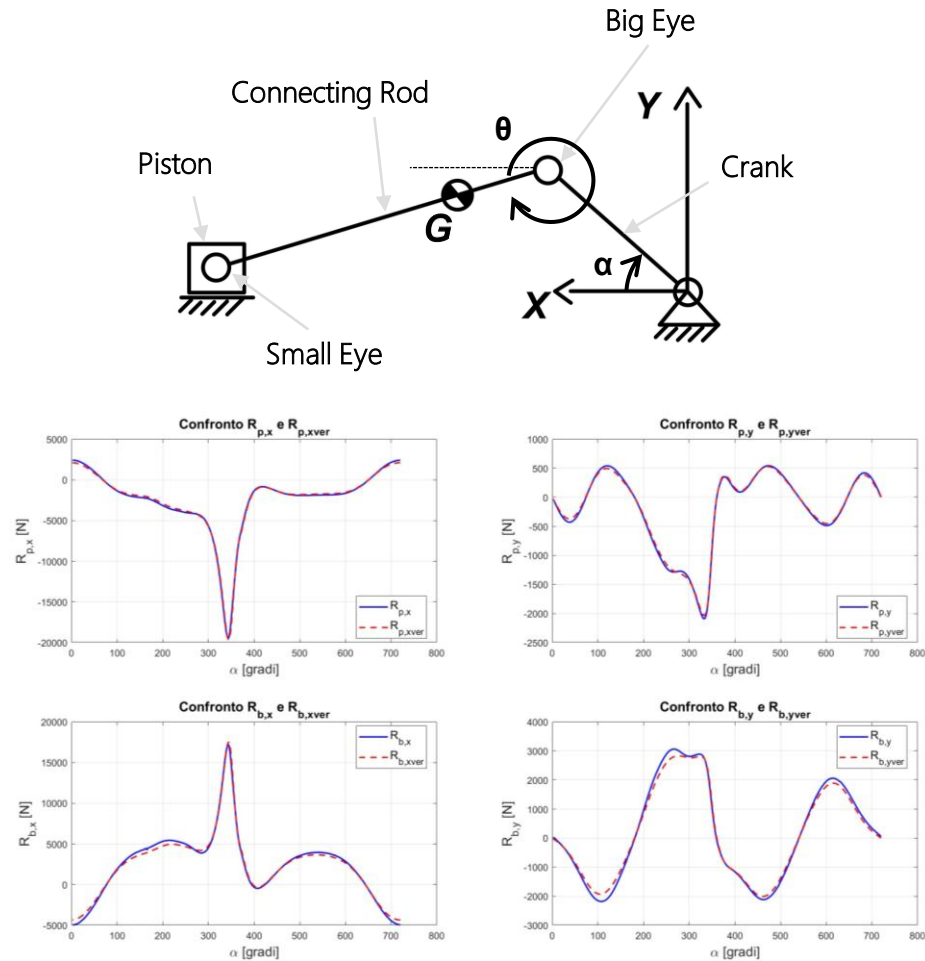
Candidato:
Danilo Lampasona

Connecting Rod Optimization

- Lower peak stress at constant mass — or same stress with less mass
- Increase safety factors and fatigue life and getting lower emissions
- Fast, reliable evaluations through a static ROM
- FEA (Ansys Workbench): stress/modal/fatigue checks
- Shape update: RBF-based mesh morphing



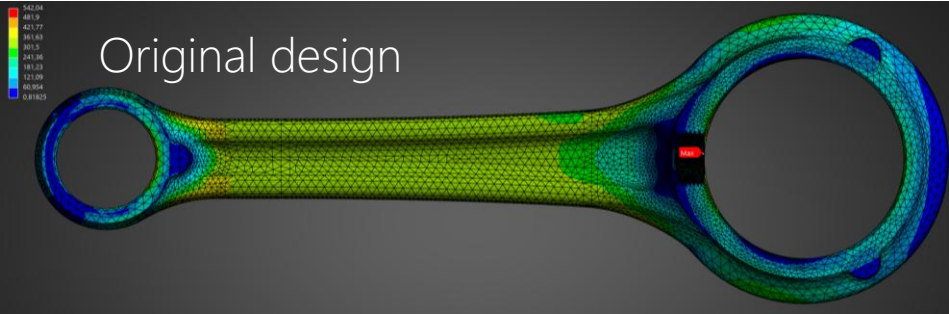
Connecting Rod Optimization



Connecting Rod Optimization

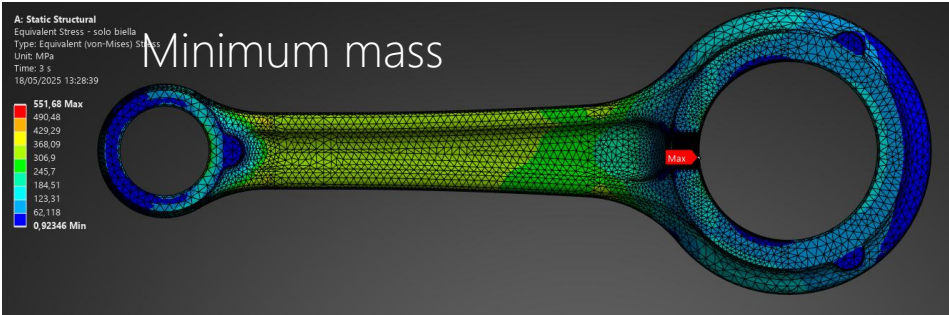
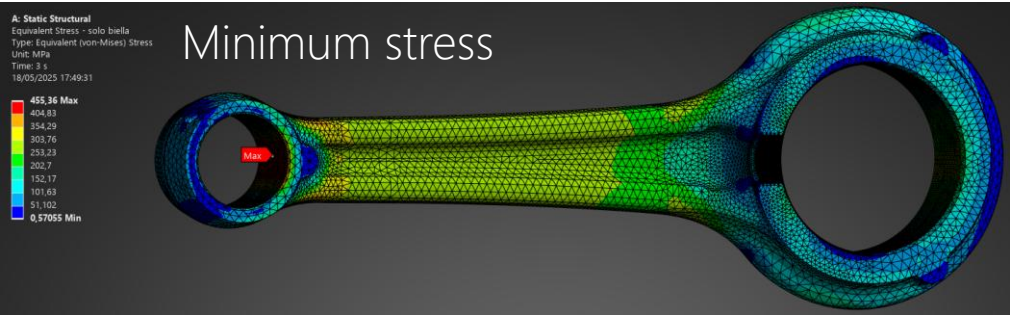


Worst load case:6500 RPM, $\alpha=344.7^\circ$, $\theta=-4.5^\circ$
 DP113: minimum stress (-17,4%)
 DP119: minimum mass (-21,0%)



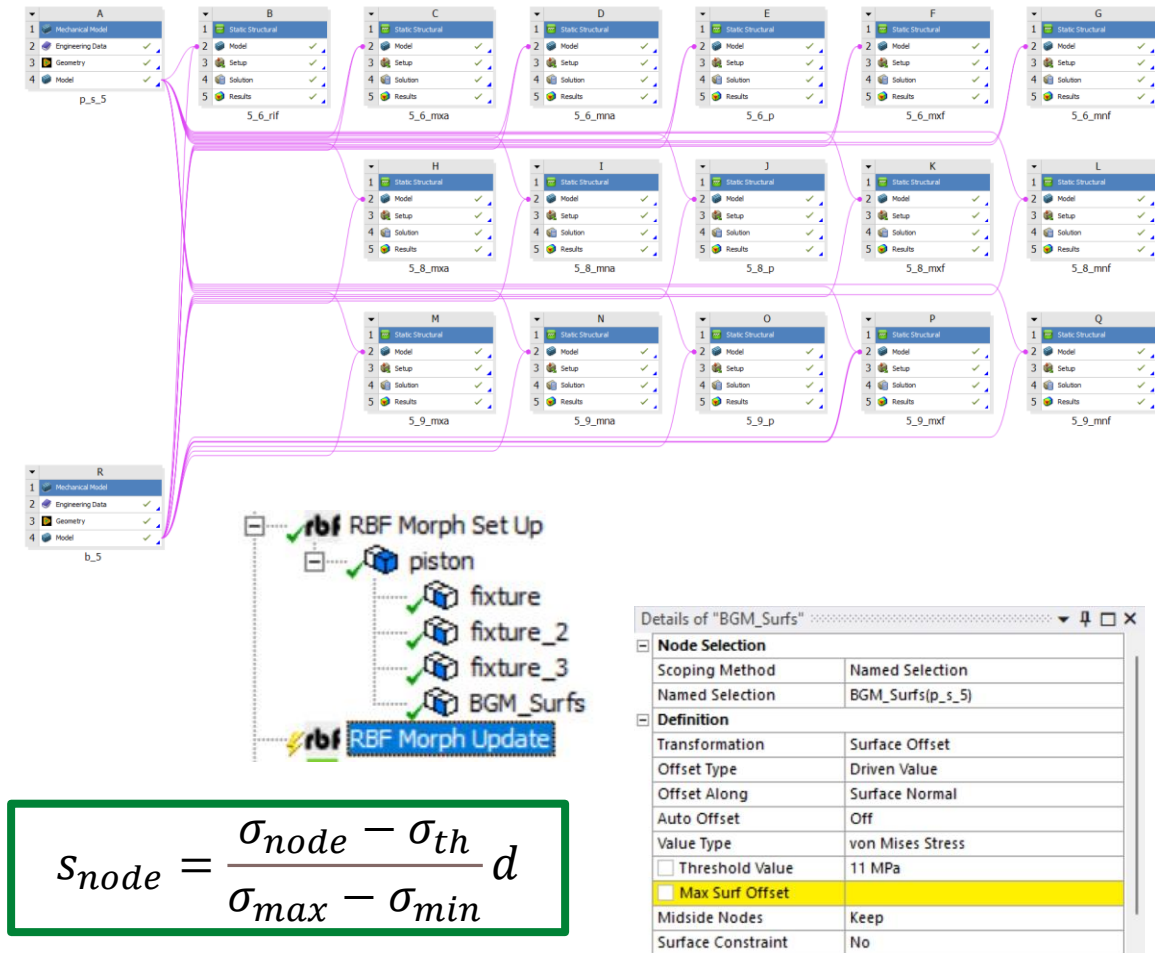
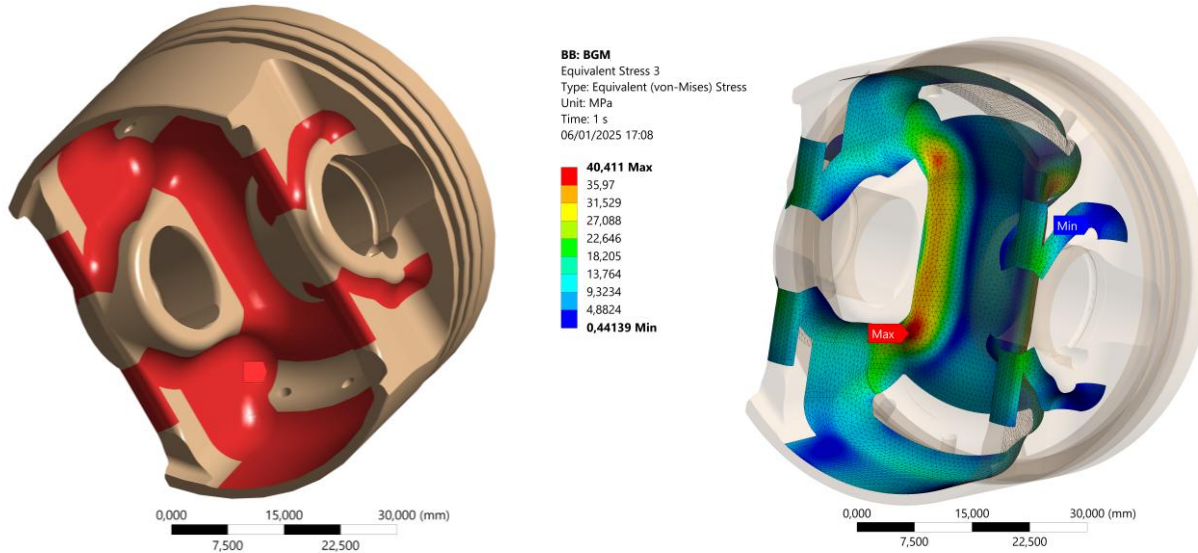
DP	P1	P2	P3	P9	P10	P11	P13
113	1.239	0.787	-0.087	1.102	0.781	0.995	0.954
119	1.218	0.765	-0.146	1.003	0.900	0.903	0.952

DP	σ_{VM} [MPa]	V_{tot} [mm ³]	$\Delta\sigma$ [MPa]	$\Delta\sigma$ [%]	ΔV [%]	Δx_G [mm]
113	455.4	18016.4	-95.6	-17.4	0.9	-0.6
119	542.0	14110.9	-9.0	-1.6	-21.0	4.4



Piston BGM Optimization

- Uniform pressure on the piston crown
- Frictionless contact between the cylinder liner and piston skirt
- Frictional contact between the wrist-pin (gudgeon pin) and the wrist-pin bore
- Fixed constraint on the inner surfaces of the wrist pin



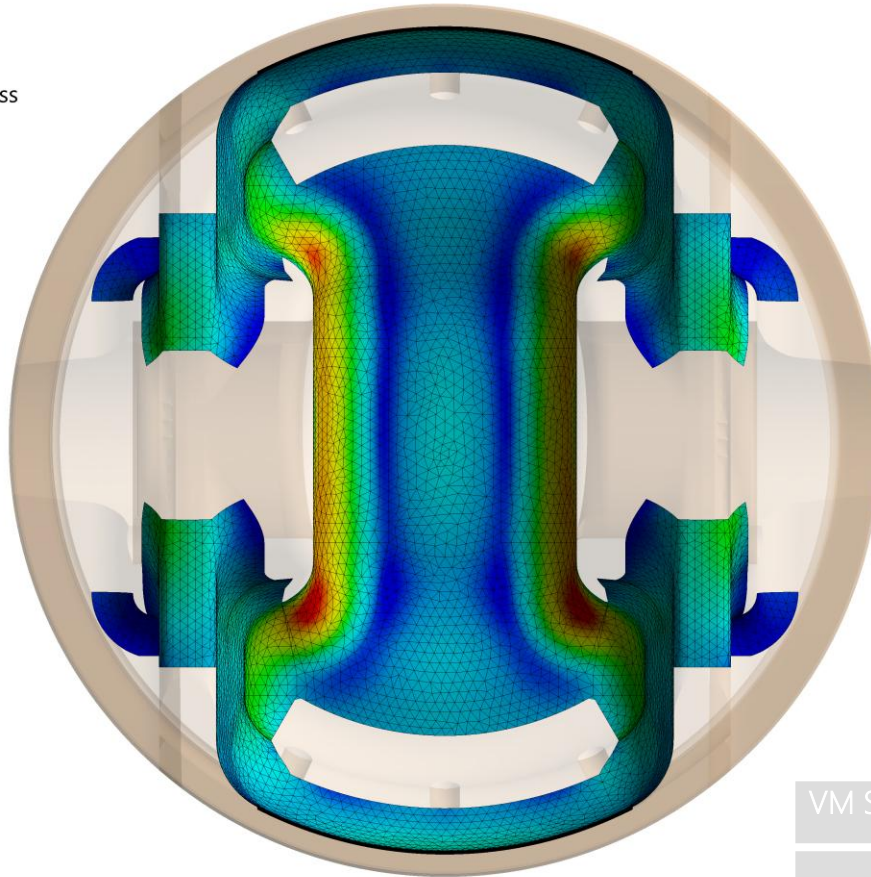
$$s_{node} = \frac{\sigma_{node} - \sigma_{th}}{\sigma_{max} - \sigma_{min}} d$$

Piston BGM Optimization - Results

BK: BGM_OptStress_0

Equivalent Stress 3
Type: Equivalent (von-Mises) Stress
Unit: MPa
Time: 1 s
06/01/2025 12:37

40,411 Max
35,97
31,529
27,088
22,646
18,205
13,764
9,3234
4,8824
0,44139 Min

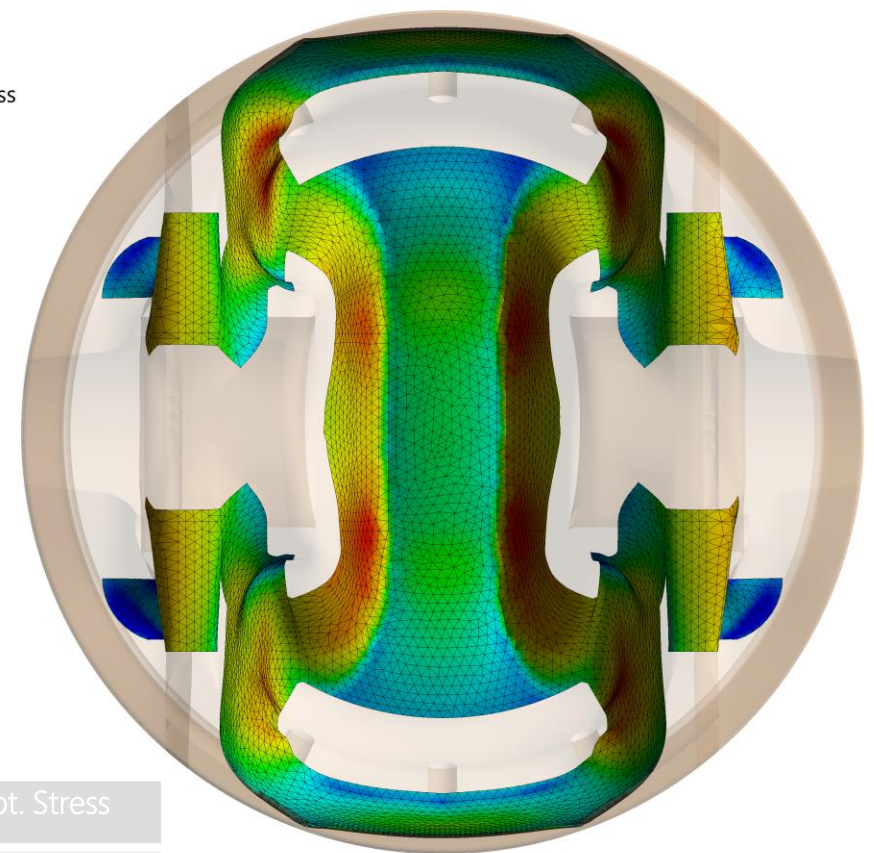


0,000 15,000 30,000 (mm)
7,500 22,500

AM: BGM_OptStress

Equivalent Stress 4
Type: Equivalent (von-Mises) Stress
Unit: MPa
Time: 1 s
06/01/2025 17:48

19,496 Max
17,518
15,54
13,561
11,583
9,605
7,6267
5,6485
3,6702
1,692 Min



0,000 15,000 30,000 (mm)
7,500 22,500

VM Stress [MPa]	Original	Opt. Stress
σ_{min}	0,44	1,69
σ_{max}	40,41	19,50
σ_{med}	11,05	11,13

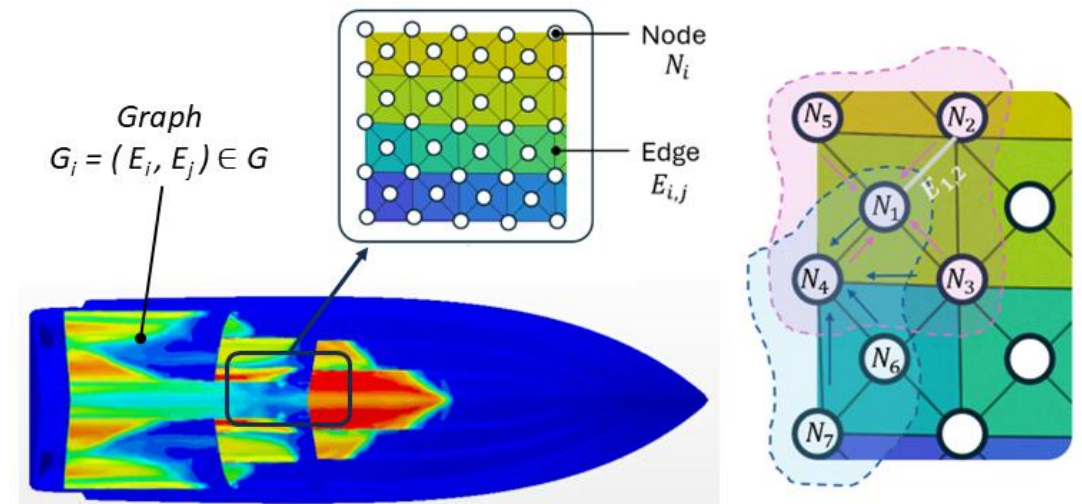
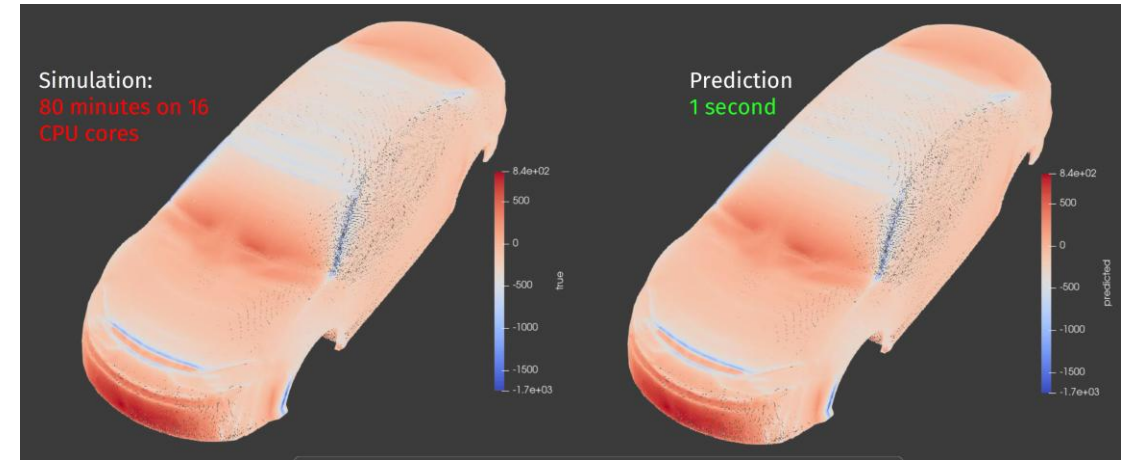
Digital Engineering

Workflows and Applications

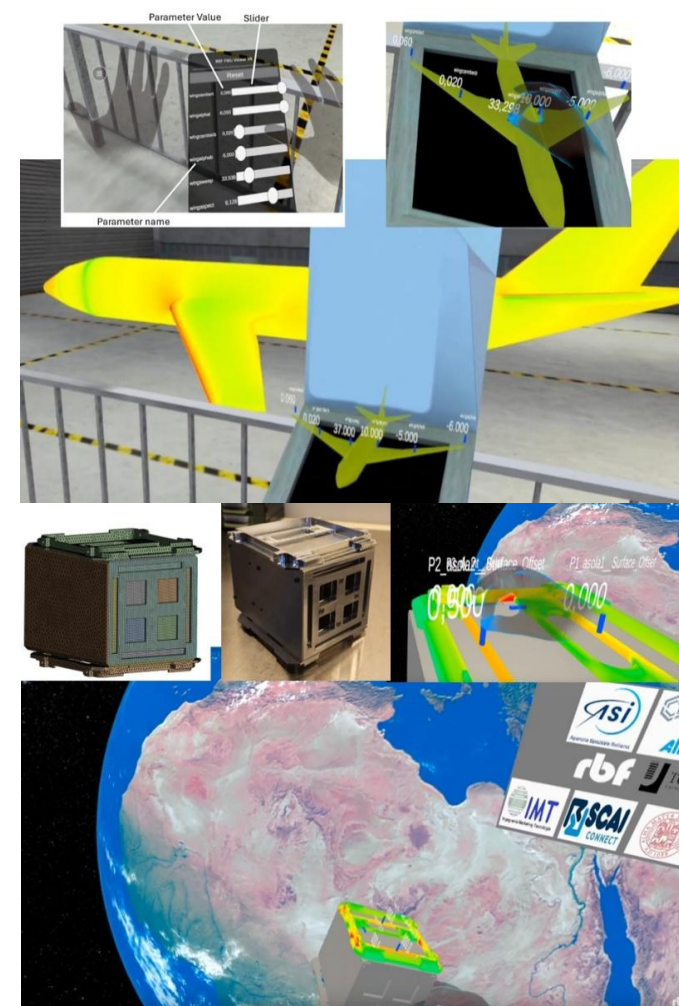
Digital Engineering Applications



- **Digital Twin** – digital replica of asset useful at design and operation
- CAE adoption is evolving: single verification, design variations, automated optimisation, **parametric space exploration** (snapshots)
- **Machine learning** is the reference for «AI» based approach
- High/medium fidelity simulations allow to generate the training data: **synthetic datasets**



Simulazione numerica: il motore dell'innovazione digitale



Connecting Rod Interactive

ROM building and validation

- 20 modes
- 80% training set, 20% validation set
- Maximum ROM error: 7%

	σ_{VM} FEM (N)	σ_{VM} ROM (N)	$\Delta\sigma_{VM}$ [%]
DP113	455.36	456.52	-0.26
DP119	542.04	566.00	-4.42

Stress (MPa)



Delete
Rename

ROM Information
Name: vonMises
Parameters (fields): 7 (0)
Learning Snapshots: 83
Output: 20 modes
Version: 2025R1
Mode: Non-linear

Export to Twin Builder

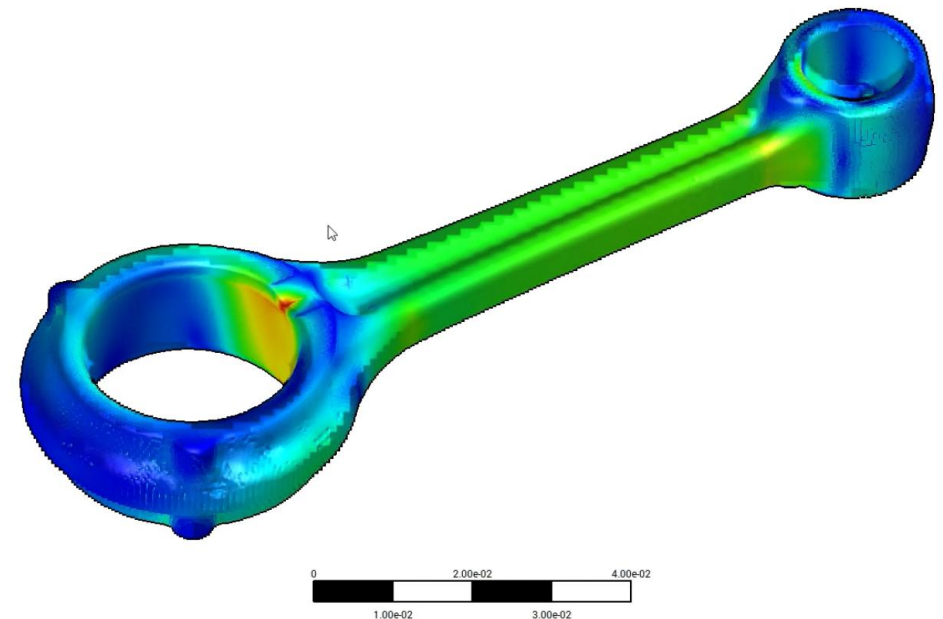
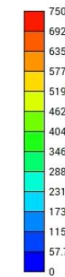
Evaluate ROM
Input parameters:

Parameter	Value
RBF Source-edges-internal Scaling y	7.56477e-01
RBF Source-edges-esterno superiore Scaling y	1.13662e+00
RBF Source-edges-esterno-l Curve Offset	-4.97975e-01
RBF Source-width Scaling y	8.52269e-01
RBF Region-rob-thickness Scaling y	7.65387e-01
RBF Source-rob-big eye Scaling x	9.36814e-01
RBF Source-rob-small eye Scaling y	9.55795e-01

Save snapshot

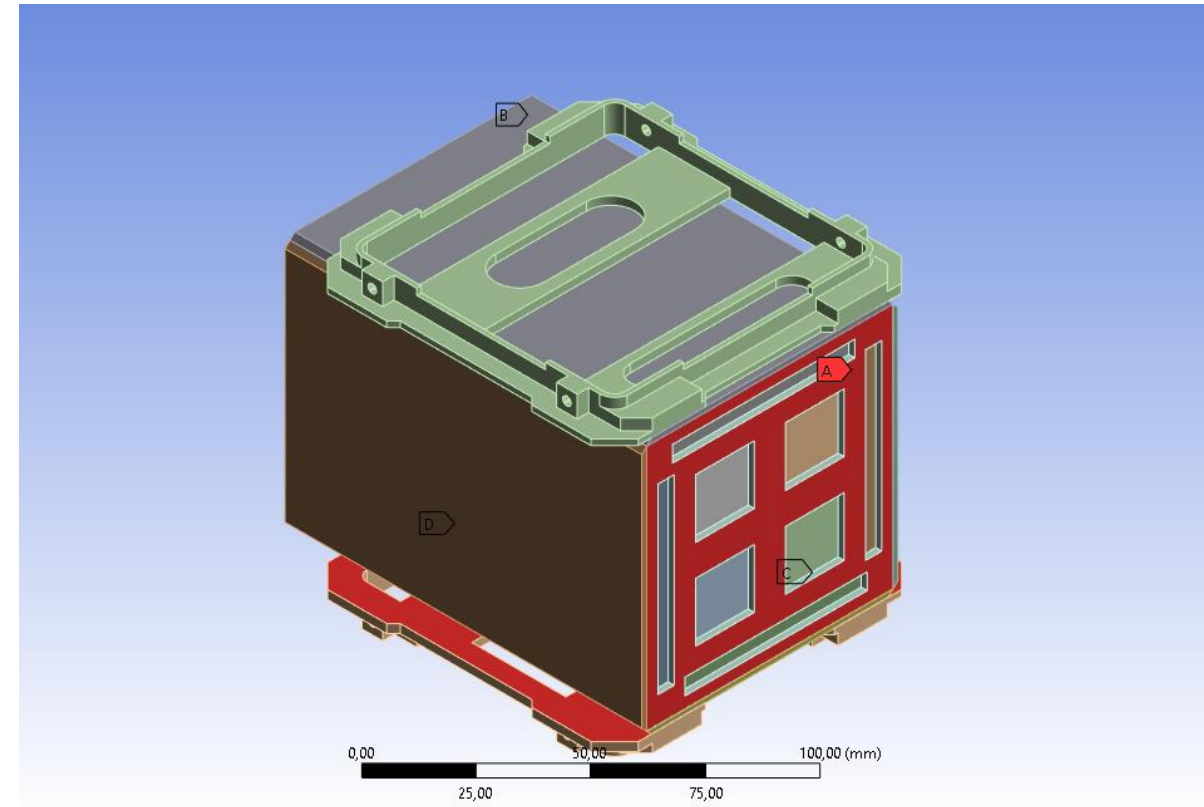
ROM Error Prediction
Reduction error - relative: 3.9 %
Interpolation error - relative: 7.5e-13 %
=> ROM error - relative: 3.9 %
=> ROM error - average absolute error: 3.7 MPa

Stress (MPa)



Thermo-Mechanical Interactive Optimization

- The **Cubesat** shown in figure is subject to two different **thermo-mechanical** load conditions
- Eyelets and thickness optimization through mesh morphing
- FEA solver: **Ansys Mechanical**



Thermo-Mechanical Interactive Optimization

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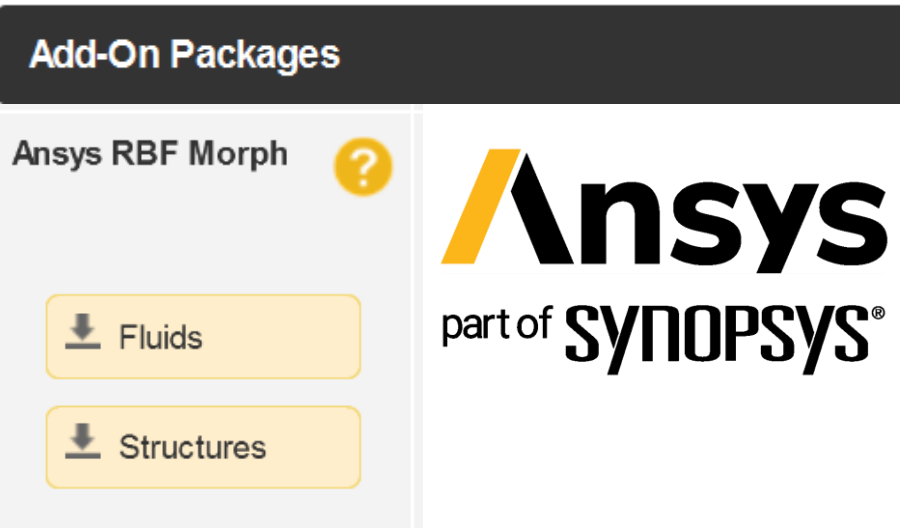
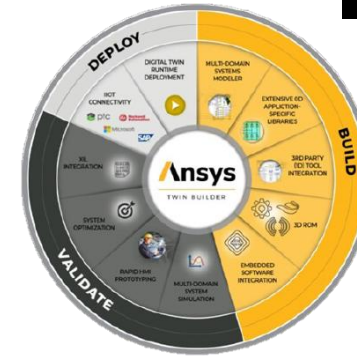


Conclusions

- Radial Basis Functions help **Digital Engineering** by providing **geometric intelligence** and an effective **inference** tool
- Parameter-free and parameter-based shape optimisation is possible
- An industrial example, fatigue optimisation of a connecting rod and a piston of a **scooter engine**, has been demonstrated
- Roadmaps toward an **AI based approach** were discussed
- Interactive VR implementation has been shown
- TRL of the solution? Everything is part of Ansys portfolio...

The advanced morphing solution selected by Ansys

- An RBF mesh morphing solution fully embedded in **Ansys**
 - **Ansys RBF Morph Fluids** – an Add On for Fluent
 - **Ansys RBF Morph Structures** – an ACT App for Mechanical
- Full integration with **optiSLang** and **Twin Builder**
- Support for **LS-DYNA** and **APDL**



Many thanks for your attention!

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youtube.com/user/RbfMorph



rbf-morph.com

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